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Penguin Enhancement and $B \rightarrow K\pi$ decays in perturbative QCD

Yong-Yeon Keum^{1,2 *}, Hsiang-nan Li^{2,3 †} and A.I. Sanda^{4‡}

¹ *Institute of Physics, Academia Sinica, Taipei, Taiwan*

² *Theory Group, KEK, Tsukuba, Ibaraki 305-0801, Japan*

³ *Department of Physics, National Cheng-Kung University,
Tainan, Taiwan 701, Republic of China*

⁴ *Department of Physics, Nagoya University, Nagoya 464-01, Japan*

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*Email: keum@phys.sinica.edu.tw

†Email: hnli@mail.ncku.edu.tw

‡Email: sanda@eken.phys.nagoya-u.ac.jp

Abstract

We compute branching ratios of $B \rightarrow K\pi$ decays in the framework of perturbative QCD factorization theorem. Decay amplitudes are classified into the topologies of tree, penguin and annihilation, all of which contain both factorizable and nonfactorizable contributions. These contributions are expressed as the convolutions of hard b quark decay amplitudes with universal meson wave functions. It is shown that (1) matrix elements of penguin operators are dynamically enhanced compared to those employed in the factorization assumption; (2) annihilation diagrams are not negligible, contrary to common belief; (3) annihilation diagrams contribute large strong phases; (4) the uncertainty of current data of the ratio $R = \text{Br}(B_d^0 \rightarrow K^\pm \pi^\mp) / \text{Br}(B^\pm \rightarrow K^0 \pi^\pm)$ and of CP asymmetries is too large to give a constraint of ϕ_3 . Assuming $\phi_3 = 90^\circ$ which is extracted from the best fit to the data of R , predictions for the branching ratios of the four $B \rightarrow K\pi$ modes are consistent with data.

1 INTRODUCTION

B factories at KEK and SLAC are taking data to probe the origin of CP violation. Within the Kobayashi-Maskawa (KM) ansatz [1], CP violation is organized in the form of a unitarity triangle shown in Fig. 1. The angle ϕ_1 can be extracted from the CP asymmetry in the $B \rightarrow J/\psi K_S$ decays, which arises from the B - \bar{B} mixing. Due to similar mechanism of CP asymmetry, the decays $B^0 \rightarrow \pi^+\pi^-$ are appropriate for the extraction of the angle ϕ_2 . However, these modes contain penguin contributions such that the extraction suffers large uncertainty. Additional measurements of the decays $B^\pm \rightarrow \pi^\pm\pi^0$ and $B^0 \rightarrow \pi^0\pi^0$ and the use of isospin symmetry may resolve the uncertainties [2]. It has been proposed that the angle ϕ_3 can be determined from the decays $B \rightarrow K\pi$, $\pi\pi$ [3, 4, 5, 6]. Contributions to these modes involve interference between penguin and tree amplitudes, and relevant strong phases have been formulated in terms of several independent parameters. We are convinced that one can not make any progress along this direction, unless he learns to compute nonleptonic two-body decay amplitudes including strong phases.

The conventional approach to exclusive nonleptonic B meson decays relies on the factorization assumption (FA) [7], in which nonfactorizable and annihilation contributions are neglected and final-state-interaction (FSI) effects are assumed to be absent. That is, this approach requires simplifying assumptions. Though analyses are easier under this assumption, estimations of many important ingredients, such as tree and penguin (including electroweak penguin) contributions, and strong phases are not reliable. Moreover, it suffers the problem of scale dependence [8]. It is also difficult to resolve some controversies in the FA approach, such as the branching ratios of the $B \rightarrow J/\psi K^{(*)}$ decays [9].

Recently, perturbative QCD (PQCD) factorization theorem for exclusive heavy-meson decays has been proved, and applied to the semileptonic $B \rightarrow D^{(*)}(\pi)l\bar{\nu}$ decays [10, 11], the nonleptonic $B \rightarrow D^{(*)}\pi(\rho)$ decays [9, 12] and the penguin-induced radiative $B \rightarrow K^*\gamma$ decays [13, 14]. PQCD is a method to separate hard components from a QCD process, which can be treated by perturbation theory. Nonperturbative components are organized in the form of hadron wave functions, which can be extracted from experimental data. Here we shall extend the PQCD formalism to more challenging charmless decays such as $B \rightarrow K\pi$, $\pi\pi$. It will

be shown that the difficulties encountered in the FA approach can be resolved in the PQCD formalism.

In this paper we shall evaluate the branching ratios of the following modes,

$$\begin{aligned} B^\pm &\rightarrow K^0 \pi^\pm, & B_d^0 &\rightarrow K^\pm \pi^\mp, \\ B^\pm &\rightarrow K^\pm \pi^0, & B_d^0 &\rightarrow K^0 \pi^0. \end{aligned} \quad (1)$$

Contributions from various topologies, such as tree, penguin and annihilation, including both factorizable and nonfactorizable contributions, can all be calculated. That is, FA is in fact not necessary. In our approach strong phases arise from non-pinched singularities of quark and gluon propagators in nonfactorizable and annihilation diagrams. As explicitly shown in Sec. VII, strong phases from the Bander-Silverman-Soni (BSS) mechanism [15], which is a source of strong phases in the FA approach, are of next-to-leading order and negligible.

As an application, we derive the ratio R and the CP asymmetries defined by

$$R = \frac{\text{Br}(B_d^0 \rightarrow K^\pm \pi^\mp)}{\text{Br}(B^\pm \rightarrow K^0 \pi^\pm)}, \quad (2)$$

$$A_{CP}^0 = \frac{\text{Br}(\bar{B}_d^0 \rightarrow K^- \pi^+) - \text{Br}(B_d^0 \rightarrow K^+ \pi^-)}{\text{Br}(\bar{B}_d^0 \rightarrow K^- \pi^+) + \text{Br}(B_d^0 \rightarrow K^+ \pi^-)}, \quad (3)$$

$$A_{CP}^c = \frac{\text{Br}(B^- \rightarrow K^0 \pi^-) - \text{Br}(B^+ \rightarrow K^0 \pi^+)}{\text{Br}(B^- \rightarrow K^0 \pi^-) + \text{Br}(B^+ \rightarrow K^0 \pi^+)}, \quad (4)$$

$$A_{CP}'^0 = \frac{\text{Br}(\bar{B}_d^0 \rightarrow K^0 \pi^0) - \text{Br}(B_d^0 \rightarrow \bar{K}^0 \pi^0)}{\text{Br}(\bar{B}_d^0 \rightarrow K^0 \pi^0) + \text{Br}(B_d^0 \rightarrow \bar{K}^0 \pi^0)}, \quad (5)$$

$$A_{CP}'^c = \frac{\text{Br}(B^- \rightarrow K^- \pi^0) - \text{Br}(B^+ \rightarrow K^+ \pi^0)}{\text{Br}(B^- \rightarrow K^- \pi^0) + \text{Br}(B^+ \rightarrow K^+ \pi^0)}, \quad (6)$$

as functions of the unitarity angle ϕ_3 using PQCD factorization theorem. In the above expressions $\text{Br}(B_d^0 \rightarrow K^\pm \pi^\mp)$ represents the CP average of the branching ratios $\text{Br}(B_d^0 \rightarrow K^+ \pi^-)$ and $\text{Br}(\bar{B}_d^0 \rightarrow K^- \pi^+)$, and the definition of $\text{Br}(B^\pm \rightarrow K^0 \pi^\pm)$ is similar. It will be shown that the uncertainty in the data for R , A_{CP}^0 and A_{CP}^c [16, 17],

$$R = 0.95 \pm 0.30, \quad A_{CP}^0 = -0.04 \pm 0.16, \quad A_{CP}^c = 0.17 \pm 0.24, \quad (7)$$

is still too large to provide useful information of ϕ_3 . Using the central values of the CLEO data for R , we obtain $\phi_3 = 90^\circ$.

An essential difference between the FA and PQCD approaches is that the hard scale at which Wilson coefficients are evaluated is chosen arbitrarily as m_b or $m_b/2$ in the former, m_b being the b quark mass, but dynamically determined in the latter. It has been shown that choosing this dynamically determined scale minimizes higher-order corrections to exclusive QCD processes [18]. We observe that this choice leads to an enhancement of penguin contributions by nearly 50% compared to those in the FA approach. As elaborated in Sec. V, this penguin enhancement is crucial for the explanation of the data of all $B \rightarrow K\pi$, $\pi\pi$ modes using a smaller angle $\phi_3 \sim 90^\circ$. Note that an angle ϕ_3 larger than 110° must be adopted in order to explain the above data in the FA approach [19].

PQCD factorization theorem for exclusive nonleptonic B meson decays are briefly reviewed in Sec. II. The factorization formulas for various $B \rightarrow K\pi$ decay modes are derived in Sec. III. The numerical analysis, including the determination of meson wave functions, is performed in Sec. IV. We emphasize the importance of the penguin enhancement in the PQCD approach in Sec. V. FSI effects are discussed in Sec. VI. The PQCD approach is compared with other approaches in Sec. VII. Section VIII is the conclusion.

2 FACTORIZATION THEOREM IN BRIEF

We first sketch the rough idea of PQCD factorization theorem and of its application to two-body B meson decays. Take the $B \rightarrow \pi$ transition form factor in the fast recoil region of the pion as an example. Obviously, this process involves two scales: the b quark mass m_b , which provides the large energy release to the fast pion, and the QCD scale Λ_{QCD} , which is associated with bound-state mesons. Therefore, the $B \rightarrow \pi$ transition form factor contains both perturbative and nonperturbative dynamics.

In perturbation theory nonperturbative dynamics is reflected by infrared divergences in radiative corrections. It has been shown order by order that these infrared divergences can be separated and absorbed into a B meson wave function or a pion wave function [10]. A formal definition of the meson wave functions as matrix elements of nonlocal operators can be constructed, which, if evaluated perturbatively, reproduces the infrared divergences. Certainly, one can not derive a wave function using a perturbative method, but has to parametrize it as

a parton model, which describes how a parton (valence quark, if a leading-twist wave function is referred) shares meson momentum. The meson wave functions, characterized by Λ_{QCD} , must be determined by nonperturbative means, such as lattice gauge theory and QCD sum rules, or extracted from experimental data. In the practical calculation below, small parton transverse momenta k_T are included, and the characteristic scale is replaced by $1/b$ with b being a variable conjugate to k_T .

After absorbing infrared divergences into the meson wave functions, the remaining part of radiative corrections is infrared finite. This part, called a hard amplitude, can be evaluated perturbatively in terms of Feynman diagrams for decays of an on-shell b quark. Note that the b quark carries various momenta, whose distribution is described by the parton model introduced above. The hard decay amplitude is characterized by the virtuality t of involved internal particles, which is of order m_b . The $B \rightarrow \pi$ transition form factor is then expressed as the convolution of three factors: the B meson and pion wave functions, and the hard b quark decay amplitude. This is so called factorization theorem. Note that the separation of nonperturbative and perturbative dynamics is quite arbitrary. This arbitrariness implies that a renormalization-group (RG) improvement of the factorization formula for the $B \rightarrow \pi$ transition form factor can be implemented. The RG evolution from the all-order summation of large logarithmic corrections to the above convolution factors will be made explicit below.

A salient feature of PQCD factorization theorem is the universality of nonperturbative wave functions. Briefly speaking, the infrared divergences associated with the B meson are process-independent, and the formal definition of the B meson wave function in terms of matrix elements of nonlocal operators is universal for all B meson decay modes. It is not difficult to understand this universality: infrared divergences correspond to long-distance effects, while the hard b quark decay occurs in a very short space-time. It is natural that these two dramatically different subprocesses decouple from each other. That is, the long-distance dynamics is insensitive to specific decays of the b quark with large energy release. Because of universality, a B meson wave function extracted from some decay modes can be employed to make predictions for other modes. This is the reason PQCD factorization theorem possesses a predictive power. We emphasize that PQCD is a theory, instead of a model, since higher-order and higher-twist

contributions can be included systematically. The model independence of PQCD predictions can be achieved, once wave functions are determined precisely.

PQCD factorization theorem for nonleptonic B meson decays, such as $B \rightarrow K(\pi)\pi$ and $B \rightarrow D^{(*)}\pi(\rho)$, is more complicated. These decays involve three scales: the W boson mass M_W , at which the matching conditions of the effective weak Hamiltonian to the full Hamiltonian are defined, the typical scale t (of order m_b) of a hard amplitude, which reflects the specific dynamics of a decay mode, and the factorization scale $1/b$ (of order Λ_{QCD}) introduced above. The dynamics below $1/b$ is regarded as being completely nonperturbative, and parametrized into meson wave functions $\phi(x, b)$, x being the momentum fraction. Above the factorization scale, radiative corrections to on-shell b quark decays can be computed perturbatively. This part contains two characteristic scales, M_W and t , differing from the case of the $B \rightarrow \pi$ transition from factor, and further factorization is necessary.

Radiative corrections produce two types of large logarithms: $\ln(M_W/t)$ and $\ln(tb)$. The former are summed by RG equations to give the evolution from M_W down to t described by the Wilson coefficients $C(t)$, while the latter are summed to give the evolution from t to $1/b$. The matching between the full Hamiltonian and the effective Hamiltonian in the above three-scale factorization theorem is similar to that in the standard effective field theory. The difference is that diagrams in the full theory contain not only W boson emissions but hard gluon emissions from spectator quarks [8]. One can show that the effective operators, in the presence of the hard gluons from spectators, still form a complete basis, and that the Wilson coefficients derived in the three-scale factorization theorem are the same as those derived in the standard effective theory.

There also exist double logarithms $\ln^2(Pb)$ from the overlap of two types of infrared divergences, collinear and soft, in radiative corrections to meson wave functions [20], where P denotes the dominant light-cone component of a meson momentum. The resummation [20, 21] of these double logarithms leads to a Sudakov form factor $\exp[-s(P, b)]$, which suppresses the long-distance contributions from the large b region, and vanishes as $b = 1/\Lambda_{\text{QCD}}$. This factor guarantees the applicability of PQCD to exclusive decays around the energy scale of the b quark mass [10]. For a detailed derivation of the relevant Sudakov form factors, we refer the

readers to [10, 11]. With all the large logarithms organized, the remaining finite contributions are absorbed into the hard b quark decay amplitude $H(t)$.

A three-scale factorization formula for exclusive nonleptonic B meson decays possesses the typical expression,

$$C(t) \otimes H(t) \otimes \phi(x, b) \otimes \exp \left[-s(P, b) - 2 \int_{1/b}^t \frac{d\bar{\mu}}{\bar{\mu}} \gamma(\alpha_s(\bar{\mu})) \right], \quad (8)$$

where the exponential involving the quark anomalous dimension $\gamma = -\alpha_s/\pi$ describes the evolution from t to $1/b$ mentioned above. Note that Eq. (8) is a convolution relation, with internal parton kinematics x and b integrated out. The hard scale t , related to the virtuality of internal particles in hard amplitudes, depends on x and b . All the convolution factors, except for the wave functions $\phi(x, b)$, are calculable in perturbation theory. The wave functions, though not calculable, are universal. If choosing t as the b quark mass m_b , the Wilson coefficient $C(m_b)$ is a constant, and Eq. (8) reduces to the simple product of the Wilson coefficient and a hadronic matrix element. However, the analysis of next-to-leading-order corrections to the pion form factor [18] has suggested that t should be chosen as the virtuality of internal particles in order to minimize higher-order corrections to the hard amplitudes.

Because of the universality of nonperturbative wave functions stated above, the strategy of PQCD factorization theorems is as follows: evaluate all perturbative factors for some decay modes, and adjust the wave functions such that predictions from the corresponding factorization formulas match experimental data. At this stage, the nonperturbative wave functions are determined up to the twist, at which the factorization is constructed. Then evaluate all the perturbative factors for another decay mode. Input the extracted wave functions into the factorization formulas of the same twist, and make predictions. With this strategy, PQCD factorization theorems are model-independent and possess a predictive power. In Sec. IV we shall make explicit the determination of the B meson, kaon, and pion wave functions from currently available data and phenomenological arguments.

3 $B \rightarrow K\pi$ AMPLITUDES

The effective Hamiltonian for the flavor-changing $b \rightarrow s$ transition is given by [22]

$$H_{\text{eff}} = \frac{G_F}{\sqrt{2}} \sum_{q=u,c} V_q \left[C_1(\mu) O_1^{(q)}(\mu) + C_2(\mu) O_2^{(q)}(\mu) + \sum_{i=3}^{10} C_i(\mu) O_i(\mu) \right], \quad (9)$$

with the Cabibbo-Kobayashi-Maskawa (CKM) matrix elements $V_q = V_{qs}^* V_{qb}$ and the operators

$$\begin{aligned} O_1^{(q)} &= (\bar{s}_i q_j)_{V-A} (\bar{q}_j b_i)_{V-A}, & O_2^{(q)} &= (\bar{s}_i q_i)_{V-A} (\bar{q}_j b_j)_{V-A}, \\ O_3 &= (\bar{s}_i b_i)_{V-A} \sum_q (\bar{q}_j q_j)_{V-A}, & O_4 &= (\bar{s}_i b_j)_{V-A} \sum_q (\bar{q}_j q_i)_{V-A}, \\ O_5 &= (\bar{s}_i b_i)_{V-A} \sum_q (\bar{q}_j q_j)_{V+A}, & O_6 &= (\bar{s}_i b_j)_{V-A} \sum_q (\bar{q}_j q_i)_{V+A}, \\ O_7 &= \frac{3}{2} (\bar{s}_i b_i)_{V-A} \sum_q e_q (\bar{q}_j q_j)_{V+A}, & O_8 &= \frac{3}{2} (\bar{s}_i b_j)_{V-A} \sum_q e_q (\bar{q}_j q_i)_{V+A}, \\ O_9 &= \frac{3}{2} (\bar{s}_i b_i)_{V-A} \sum_q e_q (\bar{q}_j q_j)_{V-A}, & O_{10} &= \frac{3}{2} (\bar{s}_i b_j)_{V-A} \sum_q e_q (\bar{q}_j q_i)_{V-A}, \end{aligned} \quad (10)$$

i, j being the color indices. Using the unitarity condition, the CKM matrix elements for the penguin operators O_3 - O_{10} can also be expressed as $V_u + V_c = -V_t$. We define the angle ϕ_3 via

$$V_{ub} = |V_{ub}| \exp(-i\phi_3). \quad (11)$$

Here we adopt the Wolfstein parametrization for the CKM matrix upto $\mathcal{O}(\lambda^3)$:

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}. \quad (12)$$

A recent analysis of quark-mixing matrix yields [23]

$$\begin{aligned} \lambda &= 0.2196 \pm 0.0023, \\ A &= 0.819 \pm 0.035, \\ R_b &\equiv \sqrt{\rho^2 + \eta^2} = 0.41 \pm 0.07. \end{aligned} \quad (13)$$

For the $B^\pm \rightarrow K^0 \pi^\pm$ decays, the operators $O_{1,2}^{(u)}$ contribute via an annihilation topology, and $O_{1,2}^{(c)}$ do not contribute at leading order of α_s . The absorptive part of the charm quark loop integral computed by BSS is thus of higher order. $O_{3,4,5,6}$ contribute via tree and annihilation

topologies, and the tree topology involves the $B \rightarrow \pi$ form factor. $O_{3,5}$ gives both factorizable and nonfactorizable (color-suppressed) contributions, while $O_{4,6}$ gives only factorizable ones because of the color flow. The contributions from $O_{7,8,9,10}$ are the same as $O_{3,4,5,6}$ except for an additional factor $(3/2)e_q$ with the light quark $q = d$ in the tree topology and with $q = u$ in the annihilation topology. For the $B_d^0 \rightarrow K^\pm \pi^\mp$ decays, the operators $O_{1,2}^{(u)}$ contribute via a tree topology, and $O_{1,2}^{(c)}$ do not contribute at leading order of α_s . The penguin operators contribute in the same way as in the $B^\pm \rightarrow K^0 \pi^\pm$ decays but with the light quark $q = u$ in the tree topology and with $q = d$ in the annihilation topology. The lowest-order hard b quark decay amplitudes are summarized in Fig. 2 for $B_d^0 \rightarrow K^\mp \pi^\pm$ decays and in Fig. 3 for $B^\pm \rightarrow \bar{K}^0 \pi^\pm$ decays.

For the $B^\pm \rightarrow K^\pm \pi^0$ decays, the operators $O_{1,2}^{(u)}$ contribute via tree and annihilation topologies, where the tree topology involves both the $B \rightarrow \pi$ and $B \rightarrow K$ form factors. The penguin operators also contribute via tree and annihilation topologies with the light quark $q = u$ in both topologies. While the tree topology involves only the $B \rightarrow \pi$ form factor. For the $B_d^0 \rightarrow K^0 \pi^0$ decays, the operators $O_{1,2}^{(u)}$ contribute via the tree topology, which involves only the $B \rightarrow K$ form factor. The penguin operators contribute in a similar way but with the light quark $q = d$ in both the tree and annihilation topologies. Their lowest-order diagrams for the hard b quark decay amplitudes are basically similar to those in Figs. 2 and 3.

The momenta of the B and K mesons in light-cone coordinates are written as $P_1 = (M_B/\sqrt{2})(1, 1, \mathbf{0}_T)$ and $P_2 = (M_B/\sqrt{2})(1, 0, \mathbf{0}_T)$, respectively. The B meson is at rest with the above parametrization of momenta. We define the momenta of light valence quark in the B meson as k_1 , where k_1 has a plus component k_1^+ , giving the momentum fraction $x_1 = k_1^+/P_1^+$, and small transverse components \mathbf{k}_{1T} . The light valence quark and the s quark in the kaon carry the longitudinal momenta $x_2 P_2$ and $(1 - x_2)P_2$, and small transverse momenta \mathbf{k}_{2T} and $-\mathbf{k}_{2T}$, respectively. The pion momentum is then $P_3 = P_1 - P_2$, whose nonvanishing component is only P_3^- . The two light valence quarks in the pion carry the longitudinal momenta $x_3 P_3$ and $(1 - x_3)P_3$, and small transverse momenta \mathbf{k}_{3T} and $-\mathbf{k}_{3T}$, respectively. The kinematic variables associated with each meson are indicated in Fig. 4.

The Sudakov resummations of the large logarithmic corrections to the B , K and π meson

wave functions ϕ_B , ϕ_K and ϕ_π lead to the exponentials $\exp(-S_B)$, $\exp(-S_K)$ and $\exp(-S_\pi)$, respectively, with the exponents [10, 24]

$$\begin{aligned} S_B(t) &= s(x_1 P_1^+, b_1) + 2 \int_{1/b_1}^t \frac{d\bar{\mu}}{\bar{\mu}} \gamma(\alpha_s(\bar{\mu})) , \\ S_K(t) &= s(x_2 P_2^+, b_2) + s((1-x_2) P_2^+, b_2) + 2 \int_{1/b_2}^t \frac{d\bar{\mu}}{\bar{\mu}} \gamma(\alpha_s(\bar{\mu})) , \\ S_\pi(t) &= s(x_3 P_3^-, b_3) + s((1-x_3) P_3^-, b_3) + 2 \int_{1/b_3}^t \frac{d\bar{\mu}}{\bar{\mu}} \gamma(\alpha_s(\bar{\mu})) . \end{aligned} \quad (14)$$

The variables b_1 , b_2 , and b_3 conjugate to the parton transverse momentum k_{1T} , k_{2T} , and k_{3T} represent the transverse extents of the B , K , and π meson, respectively. The exponent s is written as [20, 21]

$$s(Q, b) = \int_{1/b}^Q \frac{d\mu}{\mu} \left[\ln \left(\frac{Q}{\mu} \right) A(\alpha_s(\mu)) + B(\alpha_s(\mu)) \right] , \quad (15)$$

where the anomalous dimensions A to two loops and B to one loop are

$$\begin{aligned} A &= C_F \frac{\alpha_s}{\pi} + \left[\frac{67}{9} - \frac{\pi^2}{3} - \frac{10}{27} f + \frac{2}{3} \beta_0 \ln \left(\frac{e^{\gamma_E}}{2} \right) \right] \left(\frac{\alpha_s}{\pi} \right)^2 , \\ B &= \frac{2}{3} \frac{\alpha_s}{\pi} \ln \left(\frac{e^{2\gamma_E - 1}}{2} \right) , \end{aligned} \quad (16)$$

with $C_F = 4/3$ a color factor, $f = 4$ the active flavor number, and γ_E the Euler constant. The one-loop expression of the running coupling constant,

$$\alpha_s(\mu) = \frac{4\pi}{\beta_0 \ln(\mu^2/\Lambda^2)} , \quad (17)$$

is substituted into Eq. (15) with the coefficient $\beta_0 = (33 - 2f)/3$.

The decay rates of $B^\pm \rightarrow K^0 \pi^\pm$ have the expressions

$$\Gamma = \frac{G_F^2 M_B^3}{128\pi} |\mathcal{A}|^2 . \quad (18)$$

The decay amplitudes \mathcal{A}^+ and \mathcal{A}^- corresponding to $B^+ \rightarrow K^0 \pi^+$ and $B^- \rightarrow K^0 \pi^-$, respectively, are written as

$$\mathcal{A}^+ = f_K V_t^* F_e^P + V_t^* \mathcal{M}_e^P + f_B V_t^* F_a^P + V_t^* \mathcal{M}_a^P - f_B V_u^* F_a - V_u^* \mathcal{M}_a , \quad (19)$$

$$\mathcal{A}^- = f_K V_t F_e^P + V_t \mathcal{M}_e^P + f_B V_t F_a^P + V_t \mathcal{M}_a^P - f_B V_u F_a - V_u \mathcal{M}_a , \quad (20)$$

with the B meson (kaon) decay constant $f_{B(K)}$. The notations F represent factorizable contributions (form factors), and \mathcal{M} represent nonfactorizable (color-suppressed) contributions. The indices a , e and P denote the annihilation, tree and penguin topologies, respectively. F_a , associated with the time-like $K \rightarrow \pi$ form factor, and \mathcal{M}_a are from the operators $O_{1,2}^{(u)}$. The decay rates of $B_d^0 \rightarrow K^\pm \pi^\mp$ have the similar expressions with amplitudes

$$\mathcal{A} = f_K V_t^* F_e^P + V_t^* \mathcal{M}_e^P + f_B V_t^* F_a^P + V_t^* \mathcal{M}_a^P - f_K V_u^* F_e - V_u^* \mathcal{M}_e, \quad (21)$$

$$\bar{\mathcal{A}} = f_K V_t F_e^P + V_t \mathcal{M}_e^P + f_B V_t F_a^P + V_t \mathcal{M}_a^P - f_K V_u F_e - V_u \mathcal{M}_e, \quad (22)$$

for $B_d^0 \rightarrow K^+ \pi^-$ and $\bar{B}_d^0 \rightarrow K^- \pi^+$, respectively. The notations are similar to those in Eqs. (19) and (20). F_e , associated with the $B \rightarrow \pi$ form factor, and \mathcal{M}_e are from the operators $O_{1,2}^{(u)}$.

The decay amplitudes for $B^\pm \rightarrow K^\pm \pi^0$ are given by

$$\begin{aligned} \sqrt{2} \mathcal{A}'^+ &= f_K V_t^* F_e^P + V_t^* \mathcal{M}_e^P + f_B V_t^* F_a^P + V_t^* \mathcal{M}_a^P - f_B V_u^* F_a - V_u^* \mathcal{M}_a \\ &\quad - f_K V_u^* F_e - V_u^* \mathcal{M}_e - f_\pi V_u^* F_{eK} - V_u^* \mathcal{M}_{eK}, \end{aligned} \quad (23)$$

$$\begin{aligned} \sqrt{2} \mathcal{A}'^- &= f_K V_t F_e^P + V_t \mathcal{M}_e^P + f_B V_t F_a^P + V_t \mathcal{M}_a^P - f_B V_u F_a - V_u \mathcal{M}_a \\ &\quad - f_K V_u F_e - V_u \mathcal{M}_e - f_\pi V_u F_{eK} - V_u \mathcal{M}_{eK}, \end{aligned} \quad (24)$$

which correspond to $B^+ \rightarrow K^+ \pi^0$ and $B^- \rightarrow K^- \pi^0$, respectively. The factorizable contribution F_{eK} is associated with the $B \rightarrow K$ form factor, and \mathcal{M}_{eK} is the corresponding nonfactorizable contribution. Similarly, the decay rates of $B_d^0 \rightarrow K^0 \pi^0$ are obtained from the amplitudes

$$\sqrt{2} \mathcal{A}' = f_K V_t^* F_e^P + V_t^* \mathcal{M}_e^P + f_B V_t^* F_a^P + V_t^* \mathcal{M}_a^P - f_\pi V_u^* F_{eK} - V_u^* \mathcal{M}_{eK}, \quad (25)$$

$$\sqrt{2} \bar{\mathcal{A}}' = f_K V_t F_e^P + V_t \mathcal{M}_e^P + f_B V_t F_a^P + V_t \mathcal{M}_a^P - f_\pi V_u F_{eK} - V_u \mathcal{M}_{eK}, \quad (26)$$

for $B_d^0 \rightarrow K^0 \pi^0$ and $\bar{B}_d^0 \rightarrow \bar{K}^0 \pi^0$, respectively.

Basically, one needs to derive the factorization formulas only for the tree and annihilation topologies. Wilson coefficients corresponding to different operators are then inserted into the factorization formulas. The form factors are written as

$$\begin{aligned} F_e^P &= F_{e4}^P + F_{e6}^P, \\ F_{e4}^P &= 16\pi C_F M_B^2 \int_0^1 dx_1 dx_3 \int_0^\infty b_1 db_1 b_3 db_3 \phi_B(x_1, b_1) \end{aligned}$$

$$\begin{aligned} & \times \{[(1+x_3)\phi_\pi(x_3) + r_\pi(1-2x_3)\phi'_\pi(x_3)] E_{e4}(t_e^{(1)})h_e(x_1, x_3, b_1, b_3) \\ & + 2r_\pi\phi'_\pi(x_3)E_{e4}(t_e^{(2)})h_e(x_3, x_1, b_3, b_1)\} , \end{aligned} \quad (27)$$

$$\begin{aligned} F_{e6}^P &= 32\pi C_F M_B^2 \int_0^1 dx_1 dx_3 \int_0^\infty b_1 db_1 b_3 db_3 \phi_B(x_1, b_1) \\ & \times r_K \{[\phi_\pi(x_3) + r_\pi(2+x_3)\phi'_\pi(x_3)] E_{e6}(t_e^{(1)})h_e(x_1, x_3, b_1, b_3) \\ & + [x_1\phi_\pi(x_3) + 2r_\pi(1-x_1)\phi'_\pi(x_3)] E_{e6}(t_e^{(2)})h_e(x_3, x_1, b_3, b_1)\} , \end{aligned} \quad (28)$$

$$\begin{aligned} F_a^P &= F_{a4}^P + F_{a6}^P , \\ F_{a4}^P &= 16\pi C_F M_B^2 \int_0^1 dx_2 dx_3 \int_0^\infty b_2 db_2 b_3 db_3 \\ & \times \{[-x_3\phi_K(x_2)\phi_\pi(x_3) - 2r_\pi r_K(1+x_3)\phi'_K(x_2)\phi'_\pi(x_3)] E_{a4}(t_a^{(1)})h_a(x_2, x_3, b_2, b_3) \\ & + [x_2\phi_K(x_2)\phi_\pi(x_3) + 2r_\pi r_K(1+x_2)\phi'_K(x_2)\phi'_\pi(x_3)] E_{a4}(t_a^{(2)})h_a(x_3, x_2, b_3, b_2)\} , \end{aligned} \quad (29)$$

$$\begin{aligned} F_{a6}^P &= 32\pi C_F M_B^2 \int_0^1 dx_2 dx_3 \int_0^\infty b_2 db_2 b_3 db_3 \\ & \times \{[r_\pi x_3\phi_K(x_2)\phi'_\pi(x_3) + 2r_K\phi'_K(x_2)\phi_\pi(x_3)] E_{a6}(t_a^{(1)})h_a(x_2, x_3, b_2, b_3) \\ & + [2r_\pi\phi_K(x_2)\phi'_\pi(x_3) + r_K x_2\phi'_K(x_2)\phi_\pi(x_3)] E_{a6}(t_a^{(2)})h_a(x_3, x_2, b_3, b_2)\} , \end{aligned} \quad (30)$$

with the evolution factors

$$E_{ei}(t) = \alpha_s(t) a_i(t) \exp[-S_B(t) - S_\pi(t)] , \quad (31)$$

$$E_{ai}(t) = \alpha_s(t) a_i(t) \exp[-S_K(t) - S_\pi(t)] . \quad (32)$$

The expression of F_e (F_a) for the $O_{1,2}$ contributions is the same as F_{e4}^P (F_{a4}^P) but with the Wilson coefficient $a_1(t_e)$ ($a_1(t_a)$). The factorization formula of F_{eK} is written as

$$\begin{aligned} F_{eK} &= 16\pi C_F M_B^2 \int_0^1 dx_1 dx_2 \int_0^\infty b_1 db_1 b_2 db_2 \phi_B(x_1, b_1) \\ & \times \{[(1+x_2)\phi_K(x_2) + r_K(1-2x_2)\phi'_K(x_2)] E_2(t_{eK}^{(1)})h_e(x_1, x_2, b_1, b_2) \\ & + 2r_K\phi'_K(x_2)E_2(t_{eK}^{(2)})h_e(x_2, x_1, b_2, b_1)\} , \end{aligned} \quad (33)$$

with the evolution factor

$$E_2(t) = \alpha_s(t) a_2(t) \exp[-S_B(t) - S_K(t)] . \quad (34)$$

The hard functions h 's in Eqs (27)-(30) and in Eq. (33), are given by

$$h_e(x_1, x_3, b_1, b_3) = K_0(\sqrt{x_1 x_3} M_B b_1)$$

$$\begin{aligned}
& \times [\theta(b_1 - b_3) K_0(\sqrt{x_3} M_B b_1) I_0(\sqrt{x_3} M_B b_3) \\
& + \theta(b_3 - b_1) K_0(\sqrt{x_3} M_B b_3) I_0(\sqrt{x_3} M_B b_1)] , \tag{35}
\end{aligned}$$

$$\begin{aligned}
h_a(x_2, x_3, b_2, b_3) &= \left(\frac{i\pi}{2}\right)^2 H_0^{(1)}(\sqrt{x_2 x_3} M_B b_2) \\
&\times [\theta(b_2 - b_3) H_0^{(1)}(\sqrt{x_3} M_B b_2) J_0(\sqrt{x_3} M_B b_3) \\
&+ \theta(b_3 - b_2) H_0^{(1)}(\sqrt{x_3} M_B b_3) J_0(\sqrt{x_3} M_B b_2)] . \tag{36}
\end{aligned}$$

The derivation of h , from the Fourier transformation of the lowest-order H , is the same as that for the $B \rightarrow D\pi$ decays [9], but with a vanishing D meson mass. The hard scales t are chosen as the maxima of the virtualities of internal particles involved in b quark decay amplitudes, including $1/b_i$:

$$\begin{aligned}
t_e^{(1)} &= \max(\sqrt{x_3} M_B, 1/b_1, 1/b_3) , \\
t_e^{(2)} &= \max(\sqrt{x_1} M_B, 1/b_1, 1/b_3) , \\
t_a^{(1)} &= \max(\sqrt{x_3} M_B, 1/b_2, 1/b_3) , \\
t_a^{(2)} &= \max(\sqrt{x_2} M_B, 1/b_2, 1/b_3) , \\
t_{eK}^{(1)} &= \max(\sqrt{x_2} M_B, 1/b_1, 1/b_2) , \\
t_{eK}^{(2)} &= \max(\sqrt{x_1} M_B, 1/b_1, 1/b_2) , \tag{37}
\end{aligned}$$

which decrease higher-order corrections. The Sudakov factor in Eq. (14) suppresses long-distance contributions from the large b region, and improves the applicability of PQCD to B meson decays.

For the nonfactorizable amplitudes, the factorization formulas involve the kinematic variables of all the three mesons, and the Sudakov exponent is given by $S = S_B + S_K + S_\pi$. The integration over b_3 can be performed trivially, leading to $b_3 = b_1$, $b_3 = b_2$, or $b_2 = b_1$. Their expressions are

$$\begin{aligned}
\mathcal{M}_e^P &= \mathcal{M}_{e4}^P + \mathcal{M}_{e6}^P , \\
\mathcal{M}_{e4}^P &= 32\pi C_F \sqrt{2N_c} M_B^2 \int_0^1 [dx] \int_0^\infty b_1 db_1 b_2 db_2 \phi_B(x_1, b_1) \phi_K(x_2) \\
&\times \{ [(x_1 - x_2 - x_3) \phi_\pi(x_3) + r_\pi x_3 \phi'_\pi(x_3)] E'_{e4}(t_d^{(1)}) h_d^{(1)}(x_1, x_2, x_3, b_1, b_2, b_1) \\
&+ [(1 - x_1 - x_2) \phi_\pi(x_3) - r_\pi x_3 \phi'_\pi(x_3)] E'_{e4}(t_d^{(2)}) h_d^{(2)}(x_1, x_2, x_3, b_1, b_2, b_1) \} , \tag{38}
\end{aligned}$$

$$\begin{aligned}
\mathcal{M}_{e6}^P &= 32\pi C_F \sqrt{2N_c} M_B^2 \int_0^1 [dx] \int_0^\infty b_1 db_1 b_2 db_2 \phi_B(x_1, b_1) \phi'_K(x_2) \\
&\quad \times r_K \{ [(x_1 - x_2) \phi_\pi(x_3) + r_\pi(x_1 - x_2 - x_3) \phi'_\pi(x_3)] E'_{e6}(t_d^{(1)}) h_d^{(1)}(x_1, x_2, x_3, b_1, b_2, b_1) \\
&\quad + [(1 - x_1 - x_2) \phi_\pi(x_3) + r_\pi(1 - x_1 - x_2 + x_3) \phi'_\pi(x_3)] \\
&\quad \times E'_{e6}(t_d^{(2)}) h_d^{(2)}(x_1, x_2, x_3, b_1, b_2, b_1) \} , \tag{39}
\end{aligned}$$

$$\begin{aligned}
\mathcal{M}_a^P &= \mathcal{M}_{a4}^P + \mathcal{M}_{a6}^P , \\
\mathcal{M}_{a4}^P &= 32\pi C_F \sqrt{2N_c} M_B^2 \int_0^1 [dx] \int_0^\infty b_1 db_1 b_2 db_2 \phi_B(x_1, b_1) \\
&\quad \times \{ [x_3 \phi_K(x_2) \phi_\pi(x_3) - r_\pi r_K(x_1 - x_2 - x_3) \phi'_K(x_2) \phi'_\pi(x_3)] \\
&\quad \times E'_{a4}(t_f^{(1)}) h_f^{(1)}(x_1, x_2, x_3, b_1, b_2, b_2) \\
&\quad - [(x_1 + x_2) \phi_K(x_2) \phi_\pi(x_3) + r_\pi r_K(2 + x_1 + x_2 + x_3) \phi'_K(x_2) \phi'_\pi(x_3)] \\
&\quad \times E'_{a4}(t_f^{(2)}) h_f^{(2)}(x_1, x_2, x_3, b_1, b_2, b_2) \} , \tag{40}
\end{aligned}$$

$$\begin{aligned}
\mathcal{M}_{a6}^P &= 32\pi C_F \sqrt{2N_c} M_B^2 \int_0^1 [dx] \int_0^\infty b_1 db_1 b_2 db_2 \phi_B(x_1, b_1) \\
&\quad \times \{ [-r_\pi x_3 \phi_K(x_2) \phi'_\pi(x_3) - r_K(x_1 - x_2) \phi'_K(x_2) \phi_\pi(x_3)] E'_{a6}(t_f^{(1)}) h_f^{(1)}(x_1, x_2, x_3, b_1, b_2, b_2) \\
&\quad - [r_\pi(2 - x_3) \phi_K(x_2) \phi'_\pi(x_3) - r_K(2 - x_1 - x_2) \phi'_K(x_2) \phi_\pi(x_3)] \\
&\quad \times E'_{a6}(t_f^{(2)}) h_f^{(2)}(x_1, x_2, x_3, b_1, b_2, b_2) \} , \tag{41}
\end{aligned}$$

with the number of colors $N_c = 3$, the definition $[dx] \equiv dx_1 dx_2 dx_3$, and the evolution factors

$$E'_{ei}(t) = \alpha_s(t) a'_i(t) \exp[-S(t)|_{b_3=b_1}] , \tag{42}$$

$$E'_{ai}(t) = \alpha_s(t) a'_i(t) \exp[-S(t)|_{b_3=b_2}] . \tag{43}$$

The expression of \mathcal{M}_e (\mathcal{M}_a) is the same as \mathcal{M}_{e4}^P (\mathcal{M}_{a4}^P) but with the Wilson coefficient $a'_1(t_d)$ ($a'_1(t_f)$). The nonfactorizable amplitude \mathcal{M}_{eK} is written as

$$\begin{aligned}
\mathcal{M}_{eK} &= 32\pi C_F \sqrt{2N_c} M_B^2 \int_0^1 [dx] \int_0^\infty b_1 db_1 b_3 db_3 \phi_B(x_1, b_1) \phi_\pi(x_3) \\
&\quad \times \{ [(x_1 - x_2 - x_3) \phi_K(x_2) + r_K x_2 \phi'_K(x_2)] E'_2(t_{dK}^{(1)}) h_d^{(1)}(x_1, x_3, x_2, b_1, b_1, b_3) \\
&\quad + [(1 - x_1 - x_3) \phi_K(x_2) - r_K x_2 \phi'_K(x_2)] E'_2(t_{dK}^{(2)}) h_d^{(2)}(x_1, x_3, x_2, b_1, b_1, b_3) \} , \tag{44}
\end{aligned}$$

with the evolution factor

$$E'_2(t) = \alpha_s(t) a'_2(t) \exp[-S(t)|_{b_2=b_1}] . \tag{45}$$

The functions $h^{(j)}$, $j = 1$ and 2 , appearing in Eqs. (38)-(41) and in Eq. (44), are written as

$$\begin{aligned}
h_d^{(j)} &= [\theta(b_1 - b_2) K_0(DM_B b_1) I_0(DM_B b_2) \\
&\quad + \theta(b_2 - b_1) K_0(DM_B b_2) I_0(DM_B b_1)] \\
&\quad \times K_0(D_j M_B b_2), \quad \text{for } D_j^2 \geq 0, \\
&\quad \times \frac{i\pi}{2} H_0^{(1)}(\sqrt{|D_j^2|} M_B b_2), \quad \text{for } D_j^2 \leq 0,
\end{aligned} \tag{46}$$

$$\begin{aligned}
h_f^{(j)} &= \frac{i\pi}{2} [\theta(b_1 - b_2) H_0^{(1)}(FM_B b_1) J_0(FM_B b_2) \\
&\quad + \theta(b_2 - b_1) H_0^{(1)}(FM_B b_2) J_0(FM_B b_1)] \\
&\quad \times K_0(F_j M_B b_1), \quad \text{for } F_j^2 \geq 0, \\
&\quad \times \frac{i\pi}{2} H_0^{(1)}(\sqrt{|F_j^2|} M_B b_1), \quad \text{for } F_j^2 \leq 0,
\end{aligned} \tag{47}$$

with the variables

$$\begin{aligned}
D^2 &= x_1 x_3, \\
D_1^2 &= F_1^2 = (x_1 - x_2) x_3, \\
D_2^2 &= -(1 - x_1 - x_2) x_3, \\
F^2 &= x_2 x_3, \\
F_2^2 &= x_1 + x_2 + (1 - x_1 - x_2) x_3.
\end{aligned} \tag{48}$$

For details of the derivation of $h^{(j)}$, refer to [25]. The hard scales $t^{(j)}$ are chosen as

$$\begin{aligned}
t_d^{(1)} &= \max(DM_B, \sqrt{|D_1^2|} M_B, 1/b_1, 1/b_2), \\
t_d^{(2)} &= \max(DM_B, \sqrt{|D_2^2|} M_B, 1/b_1, 1/b_2), \\
t_f^{(1)} &= \max(FM_B, \sqrt{|F_1^2|} M_B, 1/b_1, 1/b_2), \\
t_f^{(2)} &= \max(FM_B, \sqrt{|F_2^2|} M_B, 1/b_1, 1/b_2), \\
t_{dK}^{(1)} &= \max(DM_B, \sqrt{|D_1^2|} M_B, 1/b_1, 1/b_3), \\
t_{dK}^{(2)} &= \max(DM_B, \sqrt{|D_2^2|} M_B, 1/b_1, 1/b_3).
\end{aligned} \tag{49}$$

In the above expressions the Wilson coefficients are defined by

$$a_1 = C_2 + \frac{C_1}{N_c},$$

$$\begin{aligned}
a'_1 &= \frac{C_1}{N_c} , \\
a_2 &= C_1 + \frac{C_2}{N_c} , \\
a'_2 &= \frac{C_2}{N_c} , \\
a_4 &= C_4 + \frac{C_3}{N_c} + \frac{3}{2}e_q \left(C_{10} + \frac{C_9}{N_c} \right) , \\
a'_4 &= \frac{1}{N_c} \left(C_3 + \frac{3}{2}e_q C_9 \right) , \\
a_6 &= C_6 + \frac{C_5}{N_c} + \frac{3}{2}e_q \left(C_8 + \frac{C_7}{N_c} \right) , \\
a'_6 &= \frac{1}{N_c} \left(C_5 + \frac{3}{2}e_q C_7 \right) .
\end{aligned} \tag{50}$$

Both QCD and electroweak penguin contributions have been included as shown in Eq. (50). The factors r_π and r_K ,

$$r_\pi = \frac{m_{0\pi}}{M_B} , \quad m_{0\pi} = \frac{M_\pi^2}{m_u + m_d} , \tag{51}$$

$$r_K = \frac{m_{0K}}{M_B} , \quad m_{0K} = \frac{M_K^2}{m_s + m_d} , \tag{52}$$

with m_u , m_d , and m_s being the masses of the u , d and s quarks, respectively, are associated with the normalizations of the pseudoscalar wave functions ϕ' . The pseudovector and pseudoscalar pion wave functions ϕ_π and ϕ'_π are defined by

$$\phi_\pi(x) = \int \frac{dy^+}{2\pi} e^{-ixP_3^- y^+} \frac{1}{2} \langle 0 | \bar{d}(y^+) \gamma^- \gamma_5 u(0) | \pi \rangle , \tag{53}$$

$$\frac{m_{0\pi}}{P_3^-} \phi'_\pi(x) = \int \frac{dy^+}{2\pi} e^{-ixP_3^- y^+} \frac{1}{2} \langle 0 | \bar{d}(y^+) \gamma_5 u(0) | \pi \rangle , \tag{54}$$

satisfying the normalization

$$\int_0^1 dx \phi_\pi(x) = \int_0^1 dx \phi'_\pi(x) = \frac{f_\pi}{2\sqrt{2N_c}} , \tag{55}$$

with the pion decay constant f_π . The kaon wave functions ϕ_K and ϕ'_K possess similar definitions and normalizations with the d quark field, m_d , M_π and f_π replaced by the s quark field, m_s , M_K and f_K , respectively.

Note that we have included the intrinsic b dependence for the heavy meson wave function ϕ_B but not for the light meson wave functions ϕ_π and ϕ_K . It has been shown that the intrinsic b

dependence of the light meson wave functions, resulting in only 4% reduction of the predictions for the $B \rightarrow \pi$ form factor, is not important [10]. It is reasonable to assume that the intrinsic b dependence of the kaon wave function, which is still unknown, is not essential either. As the transverse extent b approaches zero, the B meson wave function $\phi_B(x, b)$ reduces to the standard parton model $\phi_B(x)$, *i.e.*, $\phi_B(x) = \phi_B(x, b = 0)$, which satisfies the normalization

$$\int_0^1 \phi_B(x) dx = \frac{f_B}{2\sqrt{2N_c}}. \quad (56)$$

We do not distinguish the pseudovector and pseudoscalar components of the B meson wave functions under the heavy quark approximation. They have roughly the same normalizations because of $M_B/(m_b + m_d) \sim 1$.

4 NUMERICAL ANALYSIS

In the factorization formulas derived in Sec. IV, the Wilson coefficients evolve with the hard scale t that depends on the internal kinematic variables x_i and b_i . Wilson coefficients at a scale $\mu < M_W$ are related to the corresponding ones at $\mu = M_W$ through usual RG equations. In our analysis we adopt the leading-order expressions for the Wilson coefficients with QCD and electroweak penguins included,

$$\vec{C}(\mu) = T_g \left[\exp \left(\int_{g(M_W)}^{g(\mu)} dg' \frac{\hat{\gamma}^{(0)T}(g')}{\beta(g')} \right) \right] \cdot \vec{C}(M_W), \quad (57)$$

where the leading-order anomalous dimension matrices $\hat{\gamma}^{(0)}$ are referred to [22]. The matching conditions at $\mu = M_W$ [26] and the choices of the relevant parameters are given in Appendix A.

Since the typical scale t of a hard amplitude is smaller than the b quark mass m_b , we further evolve the Wilson coefficients from $\mu = m_b$ down to $\mu = t$ using the RG equation,

$$\mu \frac{d}{d\mu} \vec{C}(\mu) = \left[\frac{\alpha_s(\mu)}{4\pi} \hat{\gamma}_s^{(0)T} + \frac{\alpha_{em}(\mu)}{4\pi} \hat{\gamma}_e^{(0)T} \right] \cdot \vec{C}(\mu), \quad (58)$$

where the anomalous dimensions $\hat{\gamma}_{s,e}^{(0)}$ for $f = 4$ are referred to [22]. The solution to Eq. (58) and the values of the Wilson coefficients $C_i(m_b)$ are also listed in the Appendix A. For the scale t below the c quark mass $m_c = 1.5$ GeV, we still employ the evolution function with $f = 4$,

instead of with $f = 3$, for simplicity, since the matching at m_c is less essential. Therefore, we set $f = 4$ in the RG evolution between t and $1/b$ governed by the quark anomalous dimension γ .

For the B meson wave function, we adopt the model

$$\phi_B(x, b) = N_B x^2 (1-x)^2 \exp \left[-\frac{1}{2} \left(\frac{x M_B}{\omega_B} \right)^2 - \frac{\omega_B^2 b^2}{2} \right], \quad (59)$$

with the shape parameter $\omega_B = 0.4$ GeV [27]. The normalization constant N_B , which is related to the decay constant f_B , will be determined below. As to the pion wave functions, we employ the models

$$\phi_\pi(x) = \frac{3}{\sqrt{2N_c}} f_\pi x(1-x) [1 + c_\pi (5(1-2x)^2 - 1)], \quad (60)$$

$$\phi'_\pi(x) = \frac{3}{\sqrt{2N_c}} f_\pi x(1-x) [1 + c'_\pi (5(1-2x)^2 - 1)], \quad (61)$$

with the shape parameters c_π and c'_π . The kaon wave functions are chosen as

$$\phi_K(x) = \frac{3}{\sqrt{2N_c}} f_K x(1-x) [1 + 0.51(1-2x) + 0.3(5(1-2x)^2 - 1)], \quad (62)$$

$$\phi'_K(x) = \frac{3}{\sqrt{2N_c}} f_K x(1-x) [1 + c'_K (5(1-2x)^2 - 1)]. \quad (63)$$

ϕ_K is derived from QCD sum rules [28], where the second term $1 - 2x$, rendering ϕ_K a bit asymmetric, corresponds to $SU(3)$ symmetry breaking effect. The decay constant f_K is set to 160 MeV (in the convention $f_\pi = 130$ MeV). Since predictions for the $B \rightarrow K\pi$ decays are insensitive to the kaon wave functions, we simply adopt the result of QCD sum rules. For the same reason, we assume that ϕ'_K and ϕ'_π possess the same functional form and that the shape parameter c'_K of the term $5(1-2x)^2 - 1$ in ϕ'_K is equal to c'_π .

We propose to determine c_π from the branching ratios of the $B \rightarrow D\pi$ decays:

$$R_D = \frac{\text{Br}(B^- \rightarrow D^0 \pi^-)}{\text{Br}(\bar{B}_d^0 \rightarrow D^+ \pi^-)}, \quad (64)$$

because this quantity is insensitive to $m_{0\pi}$ and ϕ'_π . In order to render PQCD predictions reach the central value of the data of $R_D = 1.61$ [29], a large $c_\pi = 0.8$, which enhances nonfactorizable contributions to the $B^- \rightarrow D^0 \pi^-$ decay, is preferred. On the other hand, the data of the $B \rightarrow \rho\pi$ decays also imply a large c_π . To further enhance nonfactorizable contributions relative

to factorizable ones, the B meson wave function with $\phi_B \rightarrow x^2$ as $x \rightarrow 0$ has been assumed as shown in Eq. (59). This behavior, different from that of the model $\phi_B \rightarrow \sqrt{x}$ as $x \rightarrow 0$ proposed in [27], decreases factorizable contributions. Note that nonfactorizable contributions are insensitive to the variation of the B meson wave function. The details for the above numerical study will be published elsewhere. The extracted pion wave function ϕ_π with $c_\pi = 0.8$ is close to the Chernyak-Zhitnitsky model with $c_\pi = 1.0$ [30]. It differs from the asymptotic model with $c_\pi = 0$, which has been extracted from the data of the pion transition form factor involved in the process $\pi\gamma^* \rightarrow \gamma$ [31]. We shall argue that $\pi\gamma^* \rightarrow \gamma$ is a special process, whose infrared divergences differ from those of processes containing final-state hadrons [32]. Hence, there is no contradiction between ϕ_π determined from the $B \rightarrow D\pi$ decays and from the pion transition form factor.

We then extract c'_π from the data of the pion form factor, whose factorization formula is written as [33]

$$F_\pi(Q^2) = 16\pi C_F Q^2 \int_0^1 dx_1 dx_2 \int_0^\infty b_1 db_1 b_2 db_2 \alpha_s(t) \exp[-S_{\pi\pi}(t)] \\ \times x_2 [\phi_\pi(x_1)\phi_\pi(x_2) + 2r_\pi \phi'_\pi(x_1)\phi'_\pi(x_2)] h(x_1, x_2, b_1, b_2), \quad (65)$$

with

$$S_{\pi\pi}(t) = s(x_1 P_{\pi 1}^+, b_1) + s((1-x_1)P_{\pi 1}^+, b_1) + s(x_2 P_{\pi 2}^-, b_2) + s((1-x_2)P_{\pi 2}^-, b_2) \\ + 2 \int_{1/b_1}^t \frac{d\bar{\mu}}{\bar{\mu}} \gamma(\alpha_s(\bar{\mu})) + 2 \int_{1/b_2}^t \frac{d\bar{\mu}}{\bar{\mu}} \gamma(\alpha_s(\bar{\mu})), \quad (66)$$

$$h(x_1, x_2, b_1, b_2) = K_0(\sqrt{x_1 x_2} Q b_1) \\ \times [\theta(b_1 - b_2) K_0(\sqrt{x_2} Q b_1) I_0(\sqrt{x_2} Q b_2) \\ + \theta(b_2 - b_1) K_0(\sqrt{x_2} Q b_2) I_0(\sqrt{x_2} Q b_1)], \quad (67)$$

$$t = \max(\sqrt{x_1 x_2} Q, 1/b_1, 1/b_2). \quad (68)$$

The momentum transfer is defined by $Q^2 = 2P_{\pi 1} \cdot P_{\pi 2}$, $P_{\pi 1}$ and $P_{\pi 2}$ being the momenta of the initial and final pions, respectively. Useful references for the derivation of the above expression are [24, 34, 35]. The data are $Q^2 F_\pi(Q^2) \sim 0.4 \pm 0.2 \text{ GeV}^2$ for $Q^2 > 4 \text{ GeV}^2$ [36, 37]. Adopting the quark masses $m_u = 4.5 \text{ MeV}$ and $m_d = 1.8m_d = 8.1 \text{ MeV}$, which lead to $m_{0\pi} = 1.53 \text{ GeV}$, we find that the choice $c'_\pi = 0$ gives the pion form factor $Q^2 F_\pi(Q^2) \sim 0.4 \text{ GeV}^2$ for $Q^2 = 6.3 \text{ GeV}^2$. Hence, we choose $c'_K = c'_\pi = 0$ as stated before.

With the pion wave functions fixed in the above procedures, we determine the B meson decay constant f_B (or N_B in Eq. (59)) from the data of the $B_d^0 \rightarrow \pi^\pm \pi^\mp$ decay [17],

$$\text{Br}(B_d^0 \rightarrow \pi^\pm \pi^\mp) = (4.3_{-1.4}^{+1.6} \pm 0.5) \times 10^{-6}, \quad (69)$$

where $\text{Br}(B_d^0 \rightarrow \pi^\pm \pi^\mp)$ represents the CP average of $\text{Br}(B_d^0 \rightarrow \pi^+ \pi^-)$ and $\text{Br}(\bar{B}_d^0 \rightarrow \pi^- \pi^+)$. We employ $G_F = 1.16639 \times 10^{-5} \text{ GeV}^{-2}$, the Wolfstein parameters $\lambda = 0.2196$, $A = 0.819$, and $R_b = 0.38$, the masses $M_B = 5.28 \text{ GeV}$, and the \bar{B}_d^0 (B^-) meson lifetime $\tau_{B^0} = 1.55 \text{ ps}$ ($\tau_{B^-} = 1.65 \text{ ps}$) [23]. For the factorization formulas of the $B \rightarrow \pi\pi$ decays, refer to [38]. For the angle $\phi_3 = 90^\circ$, the result is $f_B = 190 \text{ MeV}$, which corresponds to $\text{Br}(B_d^0 \rightarrow \pi^\pm \pi^\mp) = 4.5 \times 10^{-6}$ and the $B \rightarrow \pi$ transition form factor

$$F^{B\pi}(q^2 = 0) = 0.25, \quad (70)$$

which is also reasonable. Here q stands for the momentum carried away by the external W -emission. The value of f_B is close to that adopted in the PQCD studies of the $B \rightarrow D\pi$ and $B \rightarrow K^*\gamma$ decays [13, 14], and consistent with those from lattice calculations [39] and from QCD sum rules [40] in the literature. The motivation to choose $\phi_3 = 90^\circ$ will be explained later.

We emphasize that the decay constant f_B can not be determined unambiguously in the current analysis. The above value $f_B = 190 \text{ MeV}$ corresponds to the shape parameter $\omega_B = 0.4 \text{ GeV}$. Changing ω_B , different f_B will be obtained when fitting PQCD predictions to the data in Eq. (69). However, if more data, such as the CP asymmetry in the $B_d^0 \rightarrow \pi^\pm \pi^\mp$ decays, are available, both ω_B and f_B can be uniquely determined. The reason is that tree and penguin contributions depend on ω_B and f_B simultaneously, while annihilation contributions, the most important source of strong phases as shown below, depend only on f_B . Because the branching ratio, mainly determined by tree and penguin contributions, and the CP asymmetry, related to strong phases of annihilation contributions, vary with the B meson wave function in a different way, their data can fix ω_B and f_B uniquely.

Note that the above parameters are obtained by fitting predictions to the central values of the available data. If taking into account the uncertainty of the data, the allowed range of the parameters is in fact huge. For example, any value of the shape parameter c_π in the pion

wave function ϕ_π between 0.4 and 1.0 is acceptable for the data of R_D . The shape parameter c'_K in the pseudoscalar kaon wave function ϕ'_K can differ from c'_π in ϕ'_π . In this work we do not intend to determine the range of parameters, but adopt representative parameters to make predictions for the $B \rightarrow K\pi$ decays, and examine whether the predictions are consistent with the data. For a summary of the parameters we have adopted in the numerical analysis, refer to Appendix B.

With all the meson wave functions fixed, we predict the branching ratios and the CP asymmetries of the $B \rightarrow K\pi$ decays. The s quark mass is set to $m_s = 100$ MeV, which corresponds to $m_{0K} = 2.22$ GeV. We derive the branching ratios of the four $B \rightarrow K\pi$ modes in Eq. (1) for different ϕ_3 , which are shown in Fig. 5. The branching ratios of the $K^\mp\pi^0$ and $K^\mp\pi^\pm$ modes increase with ϕ_3 , while those of the $K^0\pi^\pm$ and $K^0\pi^0$ modes are insensitive to the variation of ϕ_3 . The increase with ϕ_3 is mainly a consequence of the interference between the penguin contribution F_e^P and the tree contribution F_e . Predictions for the ratio R in Eq. (2) and the CP asymmetries A_{CP} in Eqs. (3)-(6) for different ϕ_3 are displayed in Fig. 6 and Fig. 7, respectively. The prediction of R increases from 0.7 to 1.2 when ϕ_3 moves from 0 to 180° . Unfortunately, the large uncertainty of the current data does not give a constraint of ϕ_3 . Comparing with the central value of the CLEO data of R in Eq. (7), we extract $\phi_3 = 90^\circ$. The data of A_{CP} have also large uncertainties, and do not constraint ϕ_3 either. Our analysis shows that the magnitude of A_{CP}^e and A_{CP}^0 is negligible, smaller than 3%, while the magnitude of A_{CP}^{\pm} and $A_{CP}^{\pm\prime}$ can reach 20%.

Our predictions for the branching ratio of each mode corresponding to $\phi_3 = 90^\circ$,

$$\begin{aligned}
\text{Br}(B^+ \rightarrow K^0\pi^+) &= 20.22 \times 10^{-6}, \\
\text{Br}(B^- \rightarrow \bar{K}^0\pi^-) &= 19.79 \times 10^{-6}, \\
\text{Br}(B_d^0 \rightarrow K^+\pi^-) &= 22.74 \times 10^{-6}, \\
\text{Br}(\bar{B}_d^0 \rightarrow K^-\pi^+) &= 15.50 \times 10^{-6}, \\
\text{Br}(B^+ \rightarrow K^+\pi^0) &= 11.40 \times 10^{-6}, \\
\text{Br}(B^- \rightarrow K^-\pi^0) &= 7.89 \times 10^{-6}, \\
\text{Br}(B_d^0 \rightarrow K^0\pi^0) &= 8.81 \times 10^{-6},
\end{aligned}$$

$$\text{Br}(\bar{B}_d^0 \rightarrow \bar{K}^0 \pi^0) = 9.25 \times 10^{-6} , \quad (71)$$

are consistent with the CLEO data [16],

$$\begin{aligned} \text{Br}(B^\pm \rightarrow K^0 \pi^\pm) &= (18.2_{-4.0}^{+4.6} \pm 1.6) \times 10^{-6} , \\ \text{Br}(B_d^0 \rightarrow K^\pm \pi^\mp) &= (17.2_{-2.4}^{+2.5} \pm 1.2) \times 10^{-6} , \\ \text{Br}(B^\pm \rightarrow K^\pm \pi^0) &= (11.6_{-2.7-1.3}^{+3.0+1.4}) \times 10^{-6} , \\ \text{Br}(B_d^0 \rightarrow K^0 \pi^0) &= (14.6_{-5.1-3.3}^{+5.9+2.4}) \times 10^{-6} . \end{aligned} \quad (72)$$

To derive Eq. (71), we have distinguished the pion masses $M_{\pi^\pm} = 139$ MeV and $M_{\pi^0} = 135$ MeV.

The PQCD results of each form factor and nonfactorizable amplitude involved in the $B^0 \rightarrow K^+ \pi^-$ decay are listed in Table I. It indicates that nonfactorizable contributions are only few percents of factorizable ones. This is the reason FA works well for most two-body B meson decay modes. However, there are exceptions. For modes whose factorizable contributions are proportional to the small Wilson coefficient a_2 , such as $B \rightarrow J/\psi K^{(*)}$, nonfactorizable contributions become important. Similarly, the term F_{eK} , proportional to a_2 , is small. Hence, the branching ratios of the $K\pi^0$ modes are about half of those of the $K\pi^\pm$ modes. Table I also indicates that the factorizable annihilation diagrams contribute dominant strong phases. The reason has been discussed in [41]. If expressing the amplitude of the $B_d^0 \rightarrow K^+ \pi^-$ decay as

$$\mathcal{A} \simeq V_t^* P e^{i\delta_P} - V_u^* T, \quad (73)$$

with the penguin contribution $P = |f_K F_e^P + f_B F_a^P|$ and the tree contribution $T = |f_K F_e|$, the strong phase δ_P is as large as

$$\delta_P = 144^\circ . \quad (74)$$

This result is consistent with the conclusion drawn from a global fit to data of two-body charmless B meson decays [42], where the strong phase was introduced as a free parameter.

To test the sensitivity of our predictions to different choices of model wave functions and parameters, we have varied the shape parameter ω_B for the B meson wave function from 0.3 to 0.5, the shape parameter c'_K for the kaon wave function from 0 to 0.8, the masses $m_{0K(\pi)}$ from

1.3 GeV to 2.7 GeV, the forms of the meson wave functions, such as

$$\phi_B^{\text{test}}(x, b) = N_B^{\text{test}} x(1-x) \exp \left[-\frac{1}{2} \left(\frac{xM_B}{\omega_B} \right)^2 - \frac{\omega_B^2 b^2}{2} \right], \quad (75)$$

$$\phi_K^{\text{test}}(x) = \frac{\sqrt{6}}{2} f_K x(1-x) [1 + 0.3(5(1-2x)^2 - 1)], \quad (76)$$

for the B meson and the kaon, and the asymptotic model

$$\phi_\pi^{\text{AS}}(x) = \frac{3}{\sqrt{2N_c}} f_\pi x(1-x), \quad (77)$$

for the pion, and the Wolfstein parameters λ from 0.21 to 0.22. It is found that our predictions for R change by less than 5%, and are very stable. That is, R is an appropriate quantity for the determination of ϕ_3 ,

There are other theoretical uncertainties from higher-order $O(\alpha_s^2)$ and higher-twist $O(1/M_B)$ corrections. For a simple estimation, we examine the fractional contribution to the form factor $F^{B\pi}$ as a function of $\alpha_s(t)/\pi$. It is observed that 90% and 97% of the contributions arise from the region with $\alpha_s(t)/\pi < 0.2$ and with $\alpha_s(t)/\pi < 0.3$, respectively. Therefore, our PQCD results are well within the perturbative region. It is reasonable to assume that $O(\alpha_s^2)$ corrections to the decay amplitudes are below 20%. In the derivation of the hard functions, we have neglected the mass difference $\bar{\Lambda} = M_B - m_b$ to obtain the leading-twist factorization formulas. Next-to-leading-twist corrections, proportional to $\bar{\Lambda}/M_B$, are then about 10%.

5 PENGUIN ENHANCEMENT

In this section we shall highlight the enhancement of penguin contributions observed in the PQCD approach, and its role in the explanation of the $B \rightarrow \pi\pi$ and $B \rightarrow K\pi$ data. For simplicity, we demonstrate our observation by means of the FA approach. Consider the ratios R in Eq. (2) and R_π defined by

$$R_\pi = \frac{\text{Br}(B_d^0 \rightarrow K^\pm \pi^\mp)}{\text{Br}(B_d^0 \rightarrow \pi^\pm \pi^\mp)}, \quad (78)$$

which can be written as

$$R = \frac{a_K^2 + 2a_K \lambda^2 R_b \cos \phi_3}{a_K^2}, \quad (79)$$

$$R_\pi = \frac{a_K^2 + 2a_K\lambda^2 R_b \cos \phi_3}{\lambda^2 R_b [R_b + 2a_\pi(R_b - \cos \phi_3)]} . \quad (80)$$

The factors

$$a_K = \frac{a_4 + 2r_K a_6}{a_1} , \quad a_\pi = \frac{a_4 + 2r_\pi a_6}{a_1} , \quad (81)$$

being negative values, represent the ratios of the penguin contribution to the tree contribution in the $K\pi$ and $\pi\pi$ modes, respectively. It is obvious that the data $R \sim 1$ imply $\phi_3 \sim 90^\circ$, no matter what a_K , λ and R_b are. It is the reason when we vary all the parameters in the analysis in Sec. IV, the extraction of ϕ_3 remains invariant.

While to determine ϕ_3 from the data of the ratio $R_\pi \sim 4$, one must have precise information of a_K and a_π , and of the parameters λ and R_b . It can be shown that the extraction of ϕ_3 from R_π depends on these parameters sensitively. Hence, R_π is not an appropriate quantity for the determination of ϕ_3 . To explain the data of $R_\pi \sim 4$ in the FA approach, an unreasonably large $m_0 \sim 4$ GeV corresponding to $m_d = 2m_u = 3$ MeV, *i.e.*, large $|a_{K(\pi)}| \sim 0.09$ and a large $\phi_3 \sim 130^\circ$ must be postulated [19]. This is obvious from Eq. (80), since a large $|a_{K(\pi)}|$ enhances R_π , and a large ϕ_3 leads to constructive interference between the two terms in the numerator of R_π . The determination $\phi_3 \sim 114^\circ$ from global fits to charmless B meson decays [19], located between the two extreme cases 90° and 130° , is then understood. The result of ϕ_3 will become even larger, if reasonable quark masses $m_d = 2m_u \sim 10$ MeV are employed. The huge difference between 90° and 130° extracted from different data renders the determination of ϕ_3 in the FA approach less convincing. In the modified FA approach with effective number of colors N_c^{eff} , a large unitarity angle $\phi_3 \sim 105^\circ$ is also concluded [43].

An interesting question is as follows. If we give higher weight to the extraction of ϕ_3 from R , which is more model-independent than that from R_π , can we explain the data $R_\pi \sim 4$ using a smaller ϕ_3 ? The answer is positive in the PQCD approach. Table I shows that the ratio of the penguin contribution to the tree contribution reaches

$$|a_K| = \left| \frac{F_e^P}{F_e} \right| \sim 0.1 , \quad (82)$$

even with a reasonable value of $m_0 = 1.53$ GeV. The reason is that we do not assume the same form factors for the operators $O_{1,2,3,4}$ and for $O_{5,6}$. These form factors, evaluated explicitly in

the PQCD formalism, possess different factorization formulas as shown in Eqs. (27) and (28). It is easy to observe that the integrands in the two factorization formulas become identical, if the terms associated with the pseudoscalar wave function ϕ'_π and the factors x_3 are dropped. The $x_3 \rightarrow 0$ limit corresponds to the kinematic configuration, in which the light quark emitted from the b quark decay vertex carries the full meson momentum. This is the configuration, on which the equality of the two form factors in the FA approach is constructed. Therefore, the larger ratio of the penguin contribution to the tree contribution is achieved dynamically, instead of by increasing m_0 . With this penguin enhancement, the observed branching ratios of the $B \rightarrow K\pi$ and $B \rightarrow \pi\pi$ decays and $R_\pi \sim 4$ can be explained simultaneously in the PQCD approach using $m_0 = 1.53$ GeV and a smaller $\phi_3 = 90^\circ$. That is, the data of R_π do not demand large m_0 and ϕ_3 . Such a dynamical enhancement of penguin contributions can not be obtained in the FA approach.

One of the sources responsible for the penguin enhancement is the RG evolution effect caused by the running hard scale t . In Fig. 8 we display the RG evolution of the Wilson coefficients $a_i(\mu)$, $i = 1, 4, 6$. It is found that a_1 is almost constant for $\mu = 500$ MeV to M_B . In contrast, $|a_4|$ and $|a_6|$ dramatically increase as μ evolves to below $M_B/2$. If choosing $t = M_B/2$ with $m_0 = 1.5$ GeV, the ratio $|a_{K(\pi)}| \sim 0.06$, close to that in the FA approach with the same value of m_0 , is too small to explain $R_\pi \sim 4$. As stated before, PQCD provides a prescription for choices of the hard scales t : t should be chosen as the virtualities of internal particles in Eq. (37) in order to decrease higher-order corrections. It reflects the fact that energy releases and evolution effects involved in different B meson decay modes are different. These hard scales can then reach lower values, at which $|a_6(t)|$ is enhanced over $|a_6(M_B/2)|$. This evolution effect increases $|a_{K(\pi)}|$ by about 50% as indicated by Eq. (82).

The enhancement due to the increase of $C_6(t)$ with decreasing t makes us worry that the contribution from the small t region may be important. This will invalidate the perturbative expansion of the hard amplitudes. As a check, we examine the fractional contribution to F_{e6}^P as a function of $\alpha_s(t)/\pi$. The results are displayed in Fig. 9, which indicate that about 80% (90%) of the contributions come from the region with $\alpha_s(t)/\pi < 0.2$ (0.3). Therefore, exchanged gluons are still hard enough to guarantee the applicability of PQCD.

Another source of penguin enhancement is the behavior of the B meson wave function at $x \rightarrow 0$. As shown in Eqs. (27) and (28), the factorization formulas consist of two terms. It can be easily verified that when the two terms are roughly equal, the ratio of the penguin contribution to the tree contribution reaches its maximum. A simple investigation reveals the approximate expressions of the hard functions at small momentum fractions,

$$\begin{aligned} h_e(x_1, x_3, b_1, b_3) &\sim \ln(x_1 x_3) \ln x_3, \\ h_e(x_3, x_1, b_3, b_1) &\sim \ln(x_1 x_3) \ln x_1. \end{aligned} \quad (83)$$

A B meson wave function with other behaviors, say, $\phi_B \sim x$ or \sqrt{x} [27] as $x \rightarrow 0$, leads to the dominance of the second term, and the penguin contribution becomes relatively smaller. While the B meson wave function in Eq. (59), which vanishes like x^2 as $x \rightarrow 0$, renders the contributions from the above two terms approximately the same. The penguin contribution corresponding to Eq. (59) is about 10% larger than that corresponding to the model in [27].

6 FINAL STATE INTERACTION

Two-body FSI effects have been studied in various ways [44]. It was found that these effects enhance the CP asymmetry in the $B^\pm \rightarrow K^0 \pi^\pm$ modes from order 0.5 % under the FA [45] up to order (10 - 20) %. However, Kamal has pointed out that the large CP asymmetry is due to an overestimation of FSI effects by a factor of 20 [46]. For a critic assessment on the analyses of FSI effects in the literature, refer to [46].

We briefly sketch the methods used in most of the estimates of FSI effects. For simplicity, we consider only the $B^+ \rightarrow K^0 \pi^+$ decay. The unitarity relation for the amplitude $\mathcal{A}(B^+ \rightarrow K^0 \pi^+)$ is written as

$$\text{Im } \mathcal{A}(B^+ \rightarrow K^0 \pi^+) = \frac{1}{2} \sum_N 2\pi \delta(M_B - E_N) \mathcal{A}(N \rightarrow K^0 \pi^+) \mathcal{A}^*(B^+ \rightarrow N). \quad (84)$$

If only the elastic channel $K^+ \pi^0$ contributes, Watson's theorem tells that the phase of $\mathcal{A}(B^+ \rightarrow K^0 \pi^+)$ is given by the S wave $I = 3/2$ phase shift. This argument works for the $K \rightarrow \pi\pi$ decays but not for B meson decays. For $M_B \sim 5$ GeV, many channels contribute and Watson's theorem says nothing about the strong phase of $\mathcal{A}(B^+ \rightarrow K^0 \pi^+)$. In fact, even if the phases

of $\mathcal{A}(N \rightarrow K^0\pi^+)$ for all N are known, the unitarity relation does still not fix the phase of $A(B^+ \rightarrow K^0\pi^+)$ uniquely.

Inspite of this difficulty, some authors computed $\mathcal{A}(N \rightarrow K^0\pi^+)$ for few N . Certainly, more than the unitarity relation is needed to obtain the strong phase of $A(B^+ \rightarrow K^0\pi^+)$. The phases of $\mathcal{A}(N \rightarrow K^0\pi^+)$ are often estimated by a Regge analysis. However, this method is reliable only near the forward direction. In our problem we need S wave amplitudes, *i.e.*, scattering amplitudes for all angles. A big assumption of a straight line trajectory has been adopted. This is highly questionable, especially for Pomerons. For these reasons, we believe that the above analyses are qualitative at most.

It is our viewpoint that if a strong phase can not be determined in QCD, there is no other way to compute it. A simple physical picture of FSI, the color-transparency argument, has been put forward by Bjorken [47]:

Since products of a B meson decay into two light mesons are quite energetic, the quark-antiquark pair inside a meson remains a state of small size with a correspondingly small chromomagnetic moment until it is far from the other meson. It is then more realistic that the two quark pairs group individually into final-state mesons without further exchanging soft gluons.

This picture is consistent with our observation: Sudakov suppression is strong for large meson momenta as shown in Eq. (14), which then demands final-state mesons of small transverse extent b , *i.e.*, of small chromomagnetic moment.

The effects from soft gluon exchanges among mesons in two-body heavy meson decays have been analyzed quantitatively by means of RG methods, which sum up large logarithms produced by infinite gluon emissions. It was found that these effects generate only small FSI phases for B meson decays, in agreement with the color-transparency argument, but large FSI phases for D meson decays [48]. That soft gluon effects are large in D meson decays is expected, since Sudakov suppression is weaker, two quarks in a final-state meson is separated by a larger distance, and soft gluons can resolve the color structure of that meson. Based on the above reasonings, we have neglected FSI effects in the PQCD approach to two-body B meson decays.

To justify the neglect of FSI, we apply our formalism to the $B \rightarrow \pi\pi$ and $B \rightarrow K\pi$

decays without taking into account these long-distance effects. FSI in these decays should be different. Since tree contributions dominate in the $B \rightarrow \pi\pi$ decays, extra phases from FSI do not change branching ratios very much. This argument applies to the decays $B^\pm \rightarrow K^0\pi^\pm$ and $B_d^0 \rightarrow K^0\pi^0$, where penguin contributions dominate. While the interference between tree and penguin contributions plays an essential role in the $B_d^0 \rightarrow K^\pm\pi^\mp$ and $B^\pm \rightarrow K^\pm\pi^0$ decays. Large FSI effects will change the relative phases between tree and penguin amplitudes, and thus branching ratios. If the same formalism without including FSI can be applied to both decays successfully, we believe that these long-distance effects are negligible. The agreement of our results with the data shown in Eq. (71) implies this conclusion.

Without FSI, large strong phases come from the factorizable annihilation diagrams (phases from nonfactorizable diagrams are small) in the PQCD approach as stated in Sec. IV. There has been a widely spread folklore that the annihilation diagrams give negligible contribution due to helicity suppression, the same as in $\pi \rightarrow e\bar{\nu}$ decay. That is, a left-handed massless electron and a right-handed antineutrino can not fly away back to back because of angular momentum conservation. However, this argument does not apply to F_{a6}^P . A left-handed quark and a left-handed antiquark, for which helicities are dictated by the O_6 operator, can indeed fly away back to back [49]. These behaviors have been reflected by Eqs. (29) and (30): Eq. (29) vanishes exactly, if the kaon and pion wave functions are identical, while the two terms in Eq. (30) are constructive. The reason the annihilation diagrams from the O_6 operator possess large absorptive parts can be understood in the following way. The cuts on the internal quark lines in Figs. 3(e) and 3(f) correspond to a process

$$B^+ \rightarrow \bar{s}u \rightarrow K^0\pi^+ . \quad (85)$$

The intermediate state $(\bar{s}u)$ can be regarded being highly inelastic, if expanded in terms of hadron states. According to Eq. (84), large strong phases are expected.

7 COMPARISON WITH OTHER ANALYSES

Recently, Beneke *et al.* proposed to evaluate nonfactorizable contributions to charmless B meson decays in the PQCD framework [50]. They argued that factorizable contributions (tran-

sition form factors) are not calculable in perturbation theory, but nonfactorizable contributions are. The reasoning is as follows. The internal b quark in the hard amplitude may go onto mass shell, producing a power divergent factor x^{-2} , x being the momentum fraction associated with the pion. The soft divergence from $x \rightarrow 0$ can not be removed by a pion wave function, if it vanishes like x as $x \rightarrow 0$. Since this divergence is not of the pinched type which is absorbed into a wave function, its appearance implies the breakdown of PQCD factorization theorem. While such a power divergence does not exist in nonfactorizable amplitudes [50]. We argued that the x^{-2} factor in fact can be easily smeared out by parton transverse momenta k_T considered in this work or killed by a wave function vanishing faster than x as $x \rightarrow 0$. With the inclusion of k_T and Sudakov suppression, we have explicitly shown that almost 100% of the full contribution to the $B \rightarrow \pi$ transition form factor arises from the region with the coupling constant $\alpha_s/\pi < 0.3$. It indicates that dynamics from hard gluon exchanges indeed dominate in the PQCD calculation.

There are other important differences between our approach and [50]. The momentum of the light spectator quark in the B meson has been ignored in the formalism of [50], such that quark propagators in hard nonfactorizable decay amplitudes always remain time-like. The annihilation diagrams were not included either. With these approximations, leading-order information of strong phases was lost. Strong phases then arise from diagrams of the BSS mechanism, which, as shown below, are small compared to those from annihilation diagrams. On the other hand, Sudakov resummation of large logarithmic corrections was not taken into account. It is then expected that higher-order corrections will be large and spoil the perturbative expansion. It has been shown [51] that the PQCD formalism without including Sudakov suppression is not applicable to exclusive processes for energy scale below 10 GeV.

We show that strong phases from the BSS mechanism are suppressed by the charm mass threshold and by $O(\alpha_s)$, since there must be a hard gluon emitted by the spectator as shown in Fig. 10, which turns the soft spectator in the B meson into a fast spectator in the final-state meson. That is, the contributions from the penguin diagram have been overestimated. The charm quark loop contributes an imaginary part,

$$C_2(t)\alpha_s(t) \int du u(1-u)\theta(q^2 u(1-u) - m_c^2) , \quad (86)$$

where q^2 is the invariant mass of the gluon emitted from the penguin. The contribution from the u quark loop is suppressed by the small CKM factor $|V_u|$. Since q^2 is not clearly defined in the FA approach, it is usually chosen as $q^2 = m_b^2$ or $q^2 = m_b^2/2$, and Eq. (86) gives a substantial amount of imaginary contribution to decay amplitudes [52].

However, the invariant mass q^2 can be defined unambiguously in the PQCD formalism by

$$q^2 = (x_2 P_2 + x_3 P_3)^2 = x_2 x_3 M_B^2, \quad (87)$$

since the quark going into the kaon (pion) carries the fractional momentum $x_2 P_2$ ($x_3 P_3$). Then, $q^2 = m_b^2$ or $m_b^2/2$ corresponds to a configuration, in which the two quarks produced from the gluon carry the full momenta of the two final-state mesons. Obviously, this configuration is unlikely because of the strong suppression from the kaon and pion wave functions in the large x region. Substituting Eq. (87) into Eq. (86), an exact numerical analysis indicates that the BSS mechanism contributes an imaginary part smaller than that from the nonfactorizable and annihilation amplitudes by a factor of 10. Table II shows how the imaginary part of the charm quark loop contribution vanishes with the decrease of q^2 .

On the issue of FSI, Suzuki has argued that strong phases of the $B \rightarrow K\pi$ amplitudes can not be evaluated in QCD [54]. He pointed out that the invariant masses of the $\bar{s}u$ and $\bar{d}u$ pairs in Figs. 3(c) and 3(d), respectively, are of order $(\Lambda_{\text{QCD}} M_B)^{1/2} \sim 1.2$ GeV. It implies that the $B \rightarrow K\pi$ decays are located in the resonance region and their strong phases are very complicated. We have computed the average hard scales of the $B \rightarrow K\pi$ decays, which are about 1.4 GeV, in agreement with the above estimate. However, the outgoing quark pairs possess an invariant mass larger than 1.4 GeV, such that the processes are in fact not so close to the resonance region. We could interpret that the decays occur via a six-fermion operator within space smaller than $(1/1.4)$ GeV $^{-1}$. While they are not completely short-distance, the fact that over 90% of contributions come from the x - b phase space with $\alpha_s(t)/\pi < 0.3$ allows us to estimate the decay amplitudes reliably. We believe that the strong phases can be computed up to about 20% uncertainties, which result in 30% errors in the predictions for CP asymmetries.

8 CONCLUSION

In this paper we have analyzed the $B \rightarrow K\pi$ decays using PQCD factorization theorem. In this approach hadronic matrix elements, including factorizable and nonfactorizable, and real and imaginary contributions can be evaluated explicitly. The strong phases arise from non-pinched singularities of quark and gluon propagators in annihilation and nonfactorizable hard amplitudes. It has been explicitly shown that strong phases from the BSS mechanism are small. The analysis of soft gluon effects and the simultaneous success of the PQCD applications to the $B \rightarrow K\pi$ and $B \rightarrow \pi\pi$ decays implied that long-distance FSI effects are negligible. The universal meson wave functions have been determined from the available data of the pion form factor and of the $B \rightarrow D\pi$ and $B \rightarrow \pi\pi$ decays. The dependences of the ratio R of the neutral B decay branching ratio to the charged B decay branching ratio and of the CP asymmetries on ϕ_3 have been derived. Our predictions for all the $B \rightarrow K\pi$ modes are consistent with the experimental data.

In spite of potential theoretical uncertainties, we have extracted the following features for the $B \rightarrow K\pi, \pi\pi$ decays, which are less ambiguous:

1. Nonfactorizable amplitudes are negligible.
2. Annihilation diagrams are not negligible.
3. Annihilation diagrams generate large strong phases.
4. More precise data are needed in order to obtain a strong constraint on ϕ_3 .
5. R is an ideal quantity for the determination of ϕ_3 , since it is insensitive to all the Wolfenstein and nonperturbative QCD parameters.
6. ϕ_3 is about 90° from fitting our predictions to the central value of the data of R .
7. Penguin amplitudes are dynamically enhanced, and larger than those employed in the FA approach by 50%.

8. The data of $B \rightarrow \pi\pi$ decays, *i.e.*, the ratio R_π of the $B \rightarrow K\pi$ branching ratio to the $B \rightarrow \pi\pi$ branching ratio can be explained by the smaller angle $\phi_3 \sim 90^\circ$. That is, the data of R_π do not demand a large $\phi_3 > 90^\circ$.

Acknowledgement

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APPENDIX A

In this Appendix we supply the details of the Wilson evolution. The matching conditions at $\mu = M_W$ are given by [26]

$$\begin{aligned}
C_1(M_W) &= 0, \\
C_2(M_W) &= 1, \\
C_3(M_W) &= -\frac{\alpha_s(M_W)}{24\pi} E_0(x_t) + \frac{\alpha_{em}}{6\pi} \frac{1}{\sin^2 \Theta_W} [2B_0(x_t) + C_0(x_t)], \\
C_4(M_W) &= \frac{\alpha_s(M_W)}{8\pi} E_0(x_t), \\
C_5(M_W) &= -\frac{\alpha_s(M_W)}{24\pi} E_0(x_t), \\
C_6(M_W) &= \frac{\alpha_s(M_W)}{8\pi} E_0(x_t), \\
C_7(M_W) &= \frac{\alpha_{em}}{6\pi} [4C_0(x_t) + D_0(x_t)], \\
C_8(M_W) &= 0, \\
C_9(M_W) &= \frac{\alpha_{em}}{6\pi} \left\{ 4C_0(x_t) + D_0(x_t) + \frac{1}{\sin^2 \Theta_W} [10B_0(x_t) - 4C_0(x_t)] \right\}, \\
C_{10}(M_W) &= 0,
\end{aligned} \tag{88}$$

with $x_t = m_t^2/M_W^2$, m_t being the top quark mass. The functions B_0, C_0, D_0 and E_0 are the Inami-Lim functions [53]:

$$B_0(x) = \frac{1}{4} \left[\frac{x}{1-x} + \frac{x \ln x}{(x-1)^2} \right], \tag{89}$$

$$C_0(x) = \frac{x}{8} \left[\frac{x-6}{x-1} + \frac{3x+2}{(x-1)^2} \ln x \right], \tag{90}$$

$$D_0(x) = -\frac{4}{9} \ln x - \frac{19x^3 - 25x^2}{36(x-1)^3} + \frac{x^2(5x^2 - 2x - 6)}{18(x-1)^4} \ln x, \tag{91}$$

$$E_0(x) = -\frac{2}{3} \ln x - \frac{x^2(15 - 16x + 4x^2)}{6(x-1)^4} \ln x + \frac{x(18 - 11x - x^2)}{12(1-x)^3}. \tag{92}$$

We adopt the following parameters: $m_t = 170$ GeV, $M_W = 80.2$ GeV, $\alpha_s(M_W) = 0.118$, $\alpha_{em} = 1/129$, $\sin^2 \Theta_W = 0.23$ and $\Lambda_{\overline{MS}}^{(4)} = 250$ MeV.

The solution to Eq. (58) is written as

$$\vec{C}(\mu) = U(t, m_b) \vec{C}(m_b), \tag{93}$$

The evolution function including electroweak penguins is

$$\begin{aligned}
U(t, m_b, \alpha_{em}) &= U_f(t, m_b) + \frac{\alpha_{em}}{4\pi} \int_{\ln m_b}^{\ln t} d \ln \mu' U_f(t, \mu') [\hat{\gamma}_e^{(0)T}]_f U_f(\mu', m_b) \\
&= U_f(t, M_b) + \frac{\alpha_{em}}{4\pi} R_f(t, m_b) ,
\end{aligned} \tag{94}$$

with

$$U_f(t, m_b) \equiv \exp \left[\int_{\ln m_b}^{\ln t} d \ln \mu' \frac{\alpha_s(\mu')}{4\pi} [\hat{\gamma}_s^{(0)T}]_f \right] . \tag{95}$$

For $\mu = m_b = 4.8$ GeV, the values of $C_i(m_b)$ are

$$\begin{aligned}
C_1(m_b) &= -0.271 , & C_2(m_b) &= 1.124 , \\
C_3(m_b) &= 1.255 \times 10^{-2} , & C_4(m_b) &= -2.686 \times 10^{-2} , \\
C_5(m_b) &= 7.805 \times 10^{-3} , & C_6(m_b) &= -3.287 \times 10^{-2} , \\
C_7(m_b) &= 3.453 \times 10^{-4} , & C_8(m_b) &= 3.177 \times 10^{-4} , \\
C_9(m_b) &= -9.765 \times 10^{-3} , & C_{10}(m_b) &= 2.240 \times 10^{-3} .
\end{aligned} \tag{96}$$

Values of the Wilson coefficients at different energy scales $\mu = 1.0$ GeV, 1.5 GeV, 2.0 GeV, 2.5 GeV, 3.0 GeV and 4.8 GeV are listed in Table III.

APPENDIX B

Below we summarize the parameters we have adopted in the numerical analysis of this work:

1. Masses, decay constants and lifetimes:

$$\begin{aligned}
M_{\pi^\pm} &= 0.139 \text{ GeV}, & M_{\pi^0} &= 0.135 \text{ GeV}, \\
M_K &= 0.49 \text{ GeV}, & M_B &= 5.28 \text{ GeV}, \\
m_u &= 4.5 \text{ MeV}, & m_d &= 8.1 \text{ MeV}, \\
m_s &= 100 \text{ MeV}, & m_c &= 1.5 \text{ GeV}, \\
m_b &= 4.8 \text{ GeV}, & m_t &= 170 \text{ GeV}, \\
M_W &= 80.2 \text{ GeV}, & f_B &= 190 \text{ MeV}, \\
f_\pi &= 130 \text{ MeV}, & f_K &= 160 \text{ MeV}, \\
\tau_{B^0} &= 1.55 \text{ ps}, & \tau_{B^-} &= 1.65 \text{ ps}.
\end{aligned}$$

2. QCD and electroweak parameters:

$$\begin{aligned}
G_F &= 1.16639 \times 10^{-5} \text{ GeV}^{-2}, & \Lambda_{\overline{MS}}^{(4)} &= 250 \text{ MeV}, \\
\alpha_s(M_Z) &= 0.117, & \alpha_{em} &= 1/129, \\
\lambda &= 0.2196, & A &= 0.819, \\
R_b &= \sqrt{\rho^2 + \eta^2} = 0.38.
\end{aligned}$$

3. Meson wave functions:

$$\begin{aligned}
\phi_B(x) &= N_B x^2 (1-x)^2 \exp \left[-\frac{1}{2} \left(\frac{x M_B}{\omega_B} \right)^2 - \frac{\omega_B^2 b^2}{2} \right], \\
N_B &= 91.7835 \text{ GeV}, \quad \omega_B = 0.4 \text{ GeV}, \\
\phi_\pi(x) &= \frac{3}{\sqrt{2N_c}} f_\pi x(1-x) [1 + 0.8(5(1-2x)^2 - 1)], \\
\phi'_\pi(x) &= \frac{3}{\sqrt{2N_c}} f_\pi x(1-x), \\
\phi_K(x) &= \frac{3}{\sqrt{2N_c}} f_K x(1-x) [1 + 0.51(1-2x) + 0.3(5(1-2x)^2 - 1)], \\
\phi'_K(x) &= \frac{3}{\sqrt{2N_c}} f_K x(1-x).
\end{aligned}$$

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Figure Captions

1. Fig. 1: Unitarity triangle and the definition of the angles ϕ_i .
2. Fig. 2: Feynman diagrams for the $B^\pm \rightarrow \bar{K}^0 \pi^\pm$ decays.
3. Fig. 3: Feynman diagrams for the $B_d^0 \rightarrow K^\pm \pi^\mp$ decays.
4. Fig. 4: Factorization of the $B \rightarrow K\pi$ decays in the PQCD approach.
5. Fig. 5: Dependence of the branching ratios of the $B \rightarrow K\pi$ decays on ϕ_3 with the upper (lower) dashed line corresponding to the \bar{B} (B) meson decays.
6. Fig. 6: Dependence of the ratio R on ϕ_3 . The dashed (dotted) lines correspond to the bounds (central value) of the data.
7. Fig. 7: Dependence of CP asymmetries on ϕ_3 . The dashed (dotted) lines correspond to the bounds (central value) of the data of the $B^\pm \rightarrow K^0 \pi^\pm$ decays in (a) and the $B_d^0 \rightarrow K^\pm \pi^\mp$ in (b).
8. Fig. 8: RG evolution of the Wilson coefficients $a_i(\mu)$, $i = 1, 4, 6$, normalized by their values at $\mu = m_b$.
9. Fig. 9: Fraction contribution to F_{e6}^P as a function of $\alpha_s(t)/\pi$.
10. Fig. 10: Feynman diagram for an induced c (u)-quark loop.

F_e	5.577×10^{-1}
F_e^P	-5.537×10^{-2}
F_a^P	$3.333 \times 10^{-3} + i 3.181 \times 10^{-2}$
M_e	$-0.942 \times 10^{-3} + i 3.385 \times 10^{-3}$
M_e^P	$2.931 \times 10^{-5} - i 1.304 \times 10^{-4}$
M_a^P	$-9.397 \times 10^{-5} - i 1.918 \times 10^{-4}$

Table 1: Contribution to the $B^0 \rightarrow K^+\pi^-$ decay from each form factor and nonfactorizable amplitude.

q^2	$Re[G]$	$Im[G]$
m_B^2	-0.760	2.025
$m_B^2/2$	0.139	1.775
$m_B^2/3$	0.912	1.178
$m_B^2/3.5$	1.288	0.392
$m_B^2/4$	1.162	0.000

Table 2: Real and imaginary parts of the charm quark loop contribution $G(q^2) = -4 \int du u(1-u) \ln[m_c^2 - q^2 u(1-u)]$ in the BSS mechanism.

	$\Lambda_{\overline{MS}}^{(4)} = 250 \text{ MeV}$					
μ	1.0 GeV	1.5 GeV	2.0 GeV	2.5 GeV	3.0 GeV	4.8 GeV
$\alpha_s(\mu)$	0.5439	0.4208	0.3626	0.3275	0.3034	0.2552
C_1	-0.650	-0.510	-0.435	-0.385	-0.349	-0.271
C_2	1.362	1.268	1.219	1.189	1.168	1.124
C_3	0.036	0.027	0.022	0.019	0.017	0.013
C_4	-0.063	-0.050	-0.043	-0.038	-0.035	-0.027
C_5	0.015	0.013	0.012	0.011	0.010	0.008
C_6	-0.102	-0.074	-0.060	-0.051	-0.045	-0.033
C_7/α_{em}	0.040	0.035	0.035	0.036	0.038	0.045
C_8/α_{em}	0.128	0.091	0.073	0.062	0.055	0.041
C_9/α_{em}	-1.509	-1.416	-1.366	-1.334	-1.311	-1.260
C_{10}/α_{em}	0.695	0.546	0.465	0.412	0.373	0.289

Table 3: Values of the running coupling constant α_s and the Wilson coefficients C_i with $\Lambda_{\overline{MS}}^{(4)} = 250 \text{ MeV}$ for different energy scales $\mu = 1.0, 1.5, 2.0, 2.5, 3.0$, and 4.8 GeV .

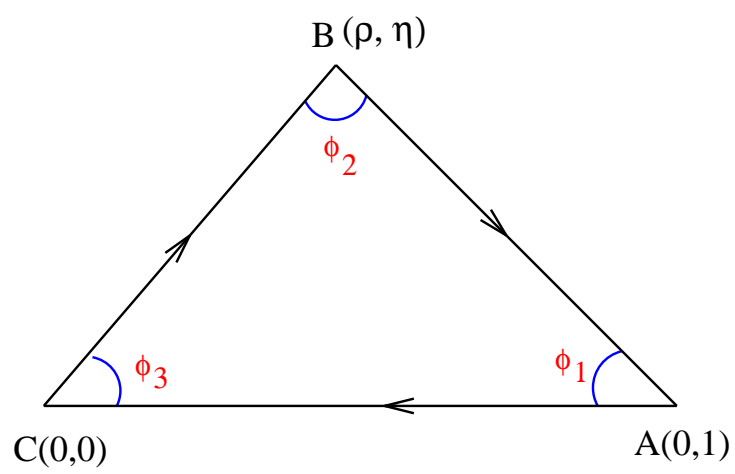


Figure 1:

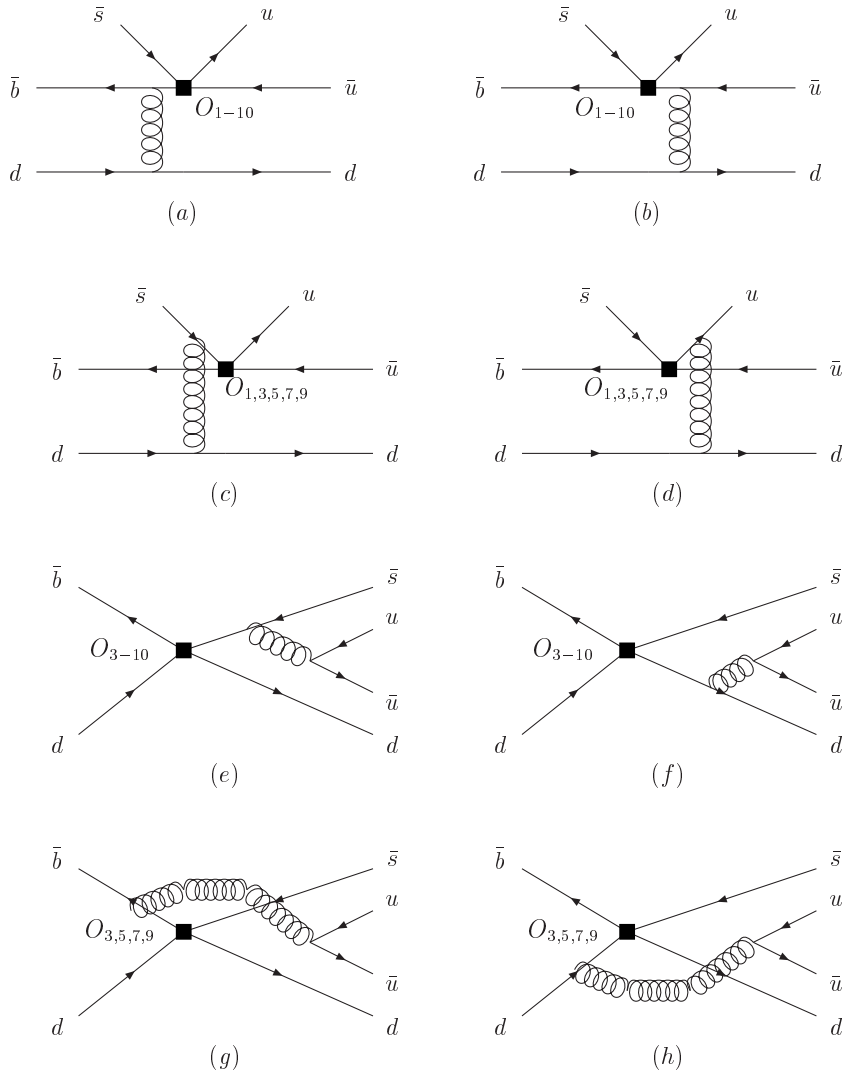


Figure 2:

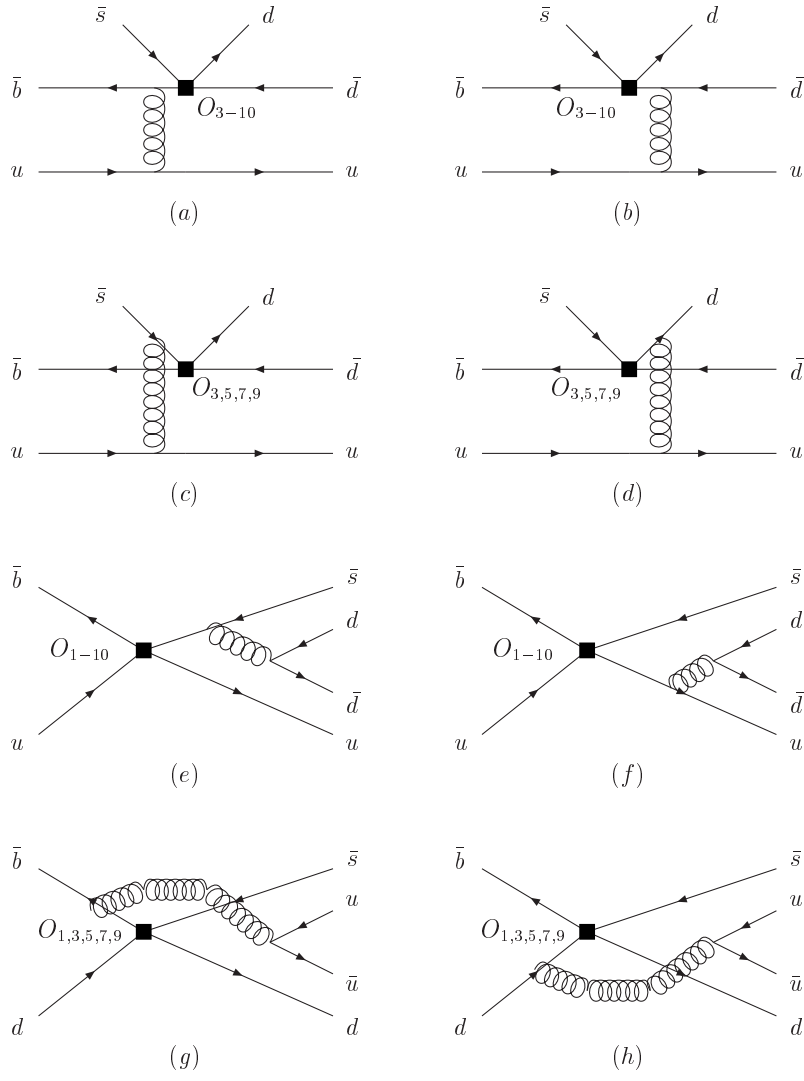


Figure 3:

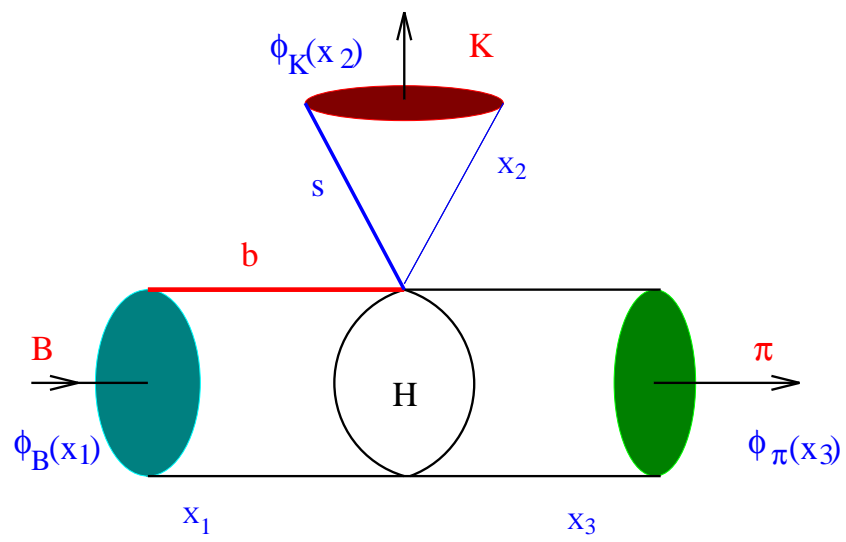


Figure 4:

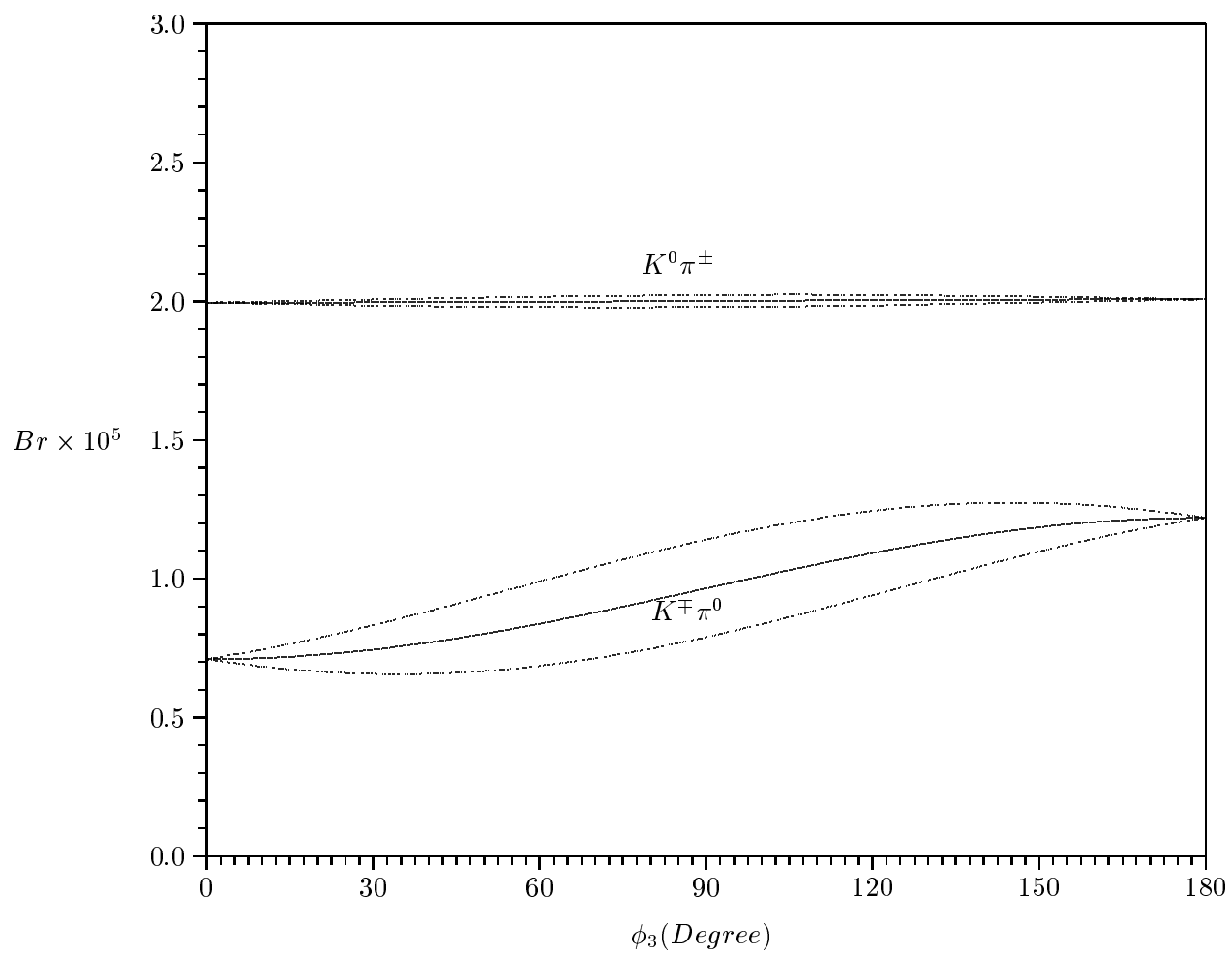


Figure 5(a)

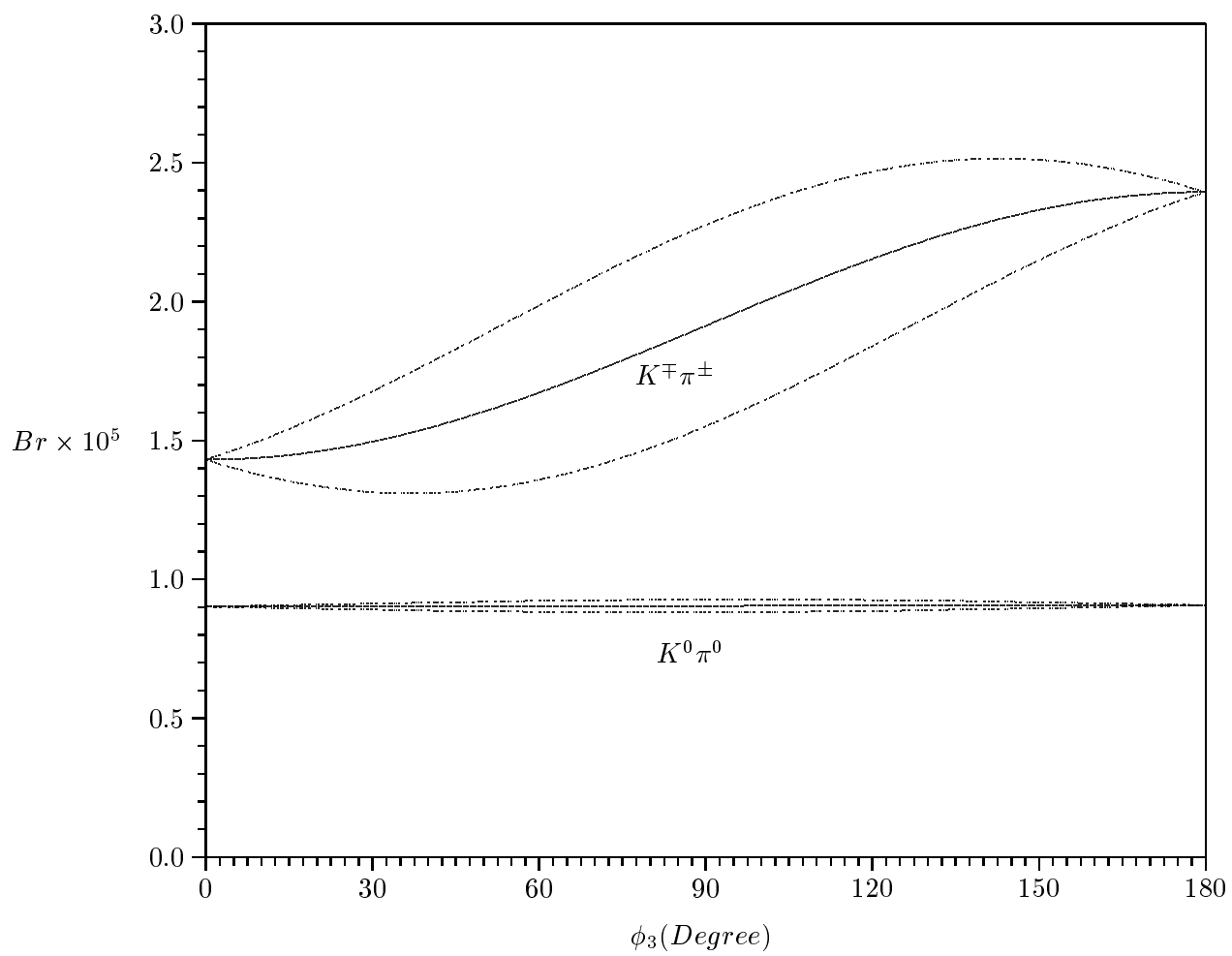


Figure 5(b)

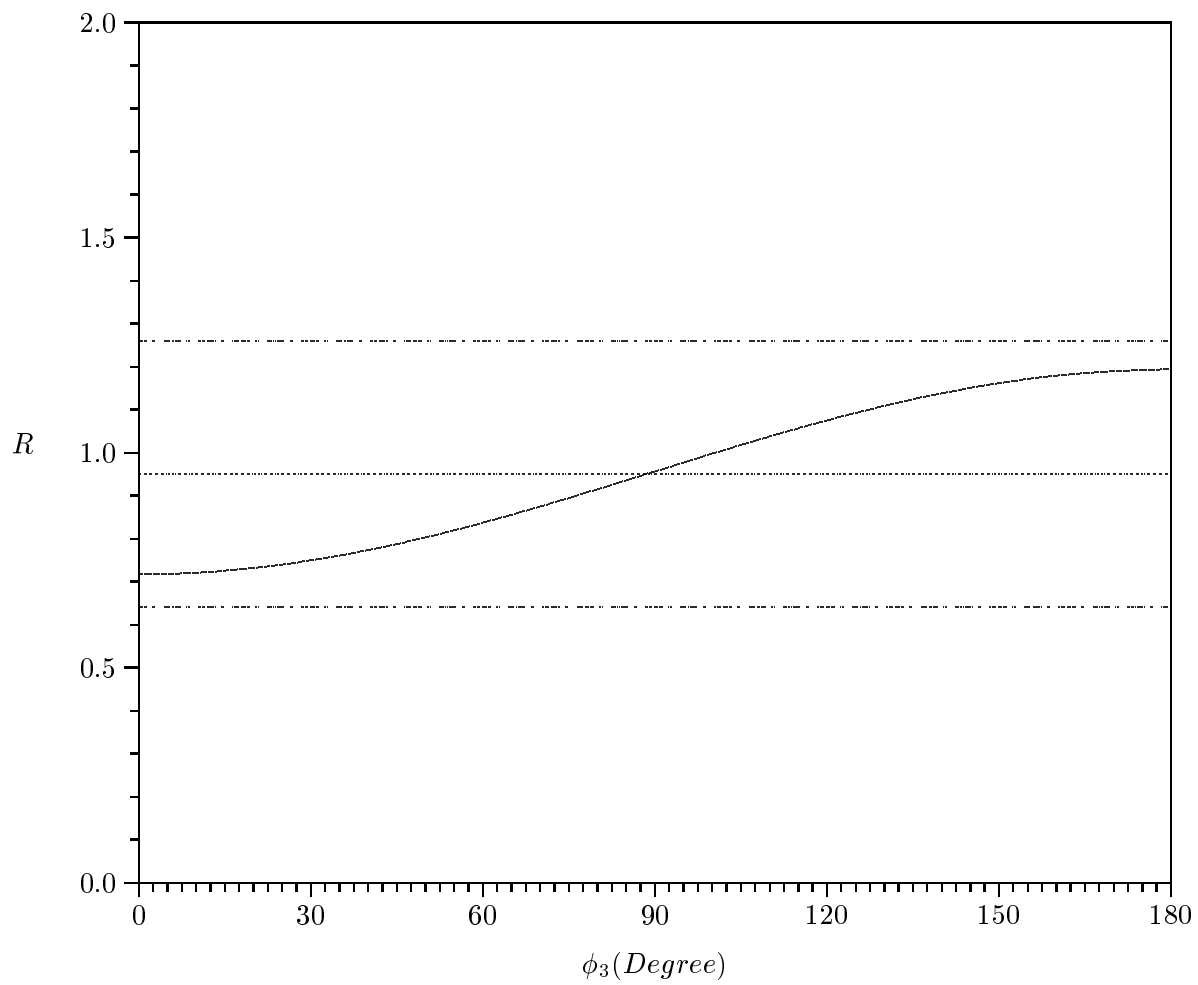


Figure 6

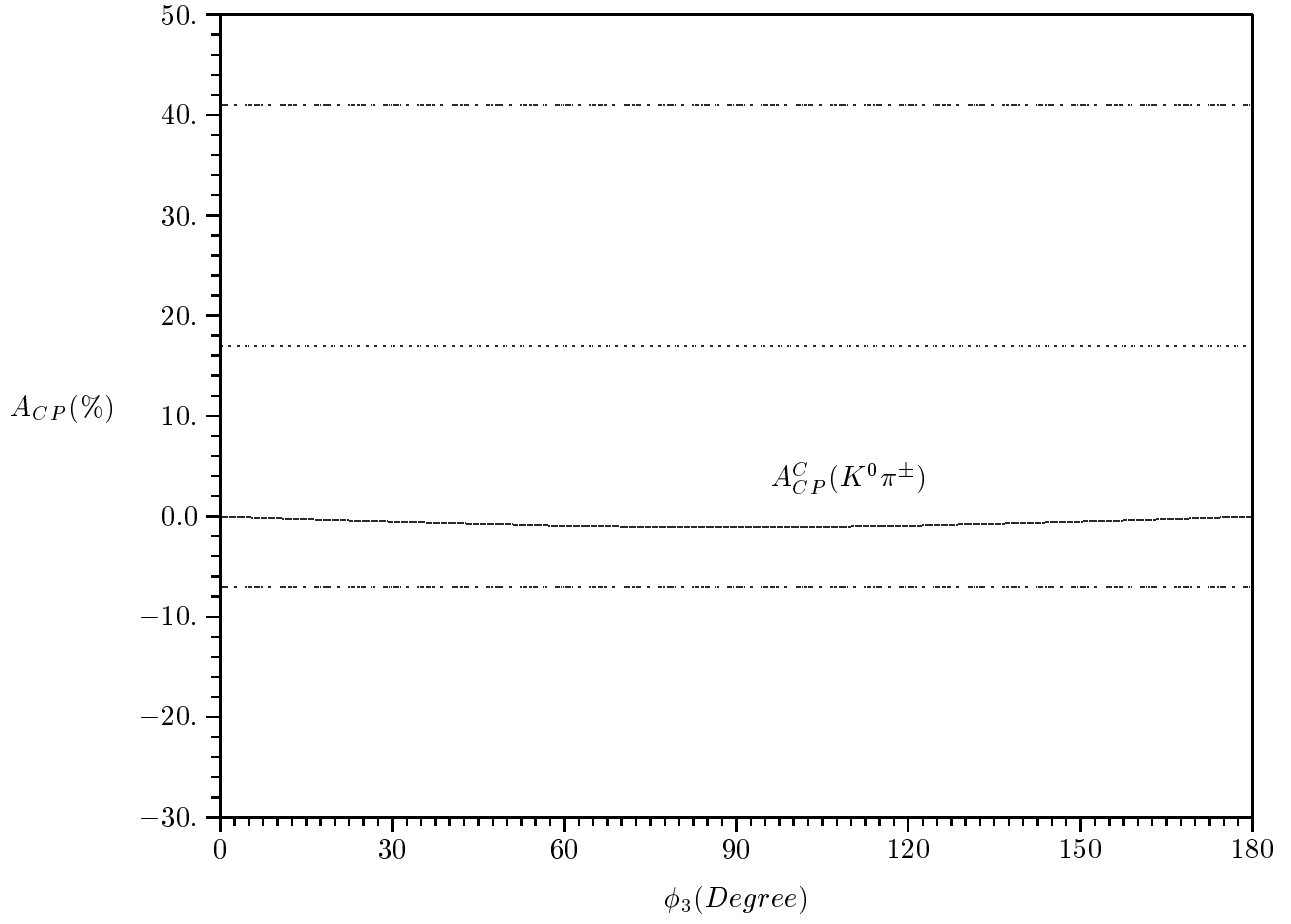


Figure 7(a)

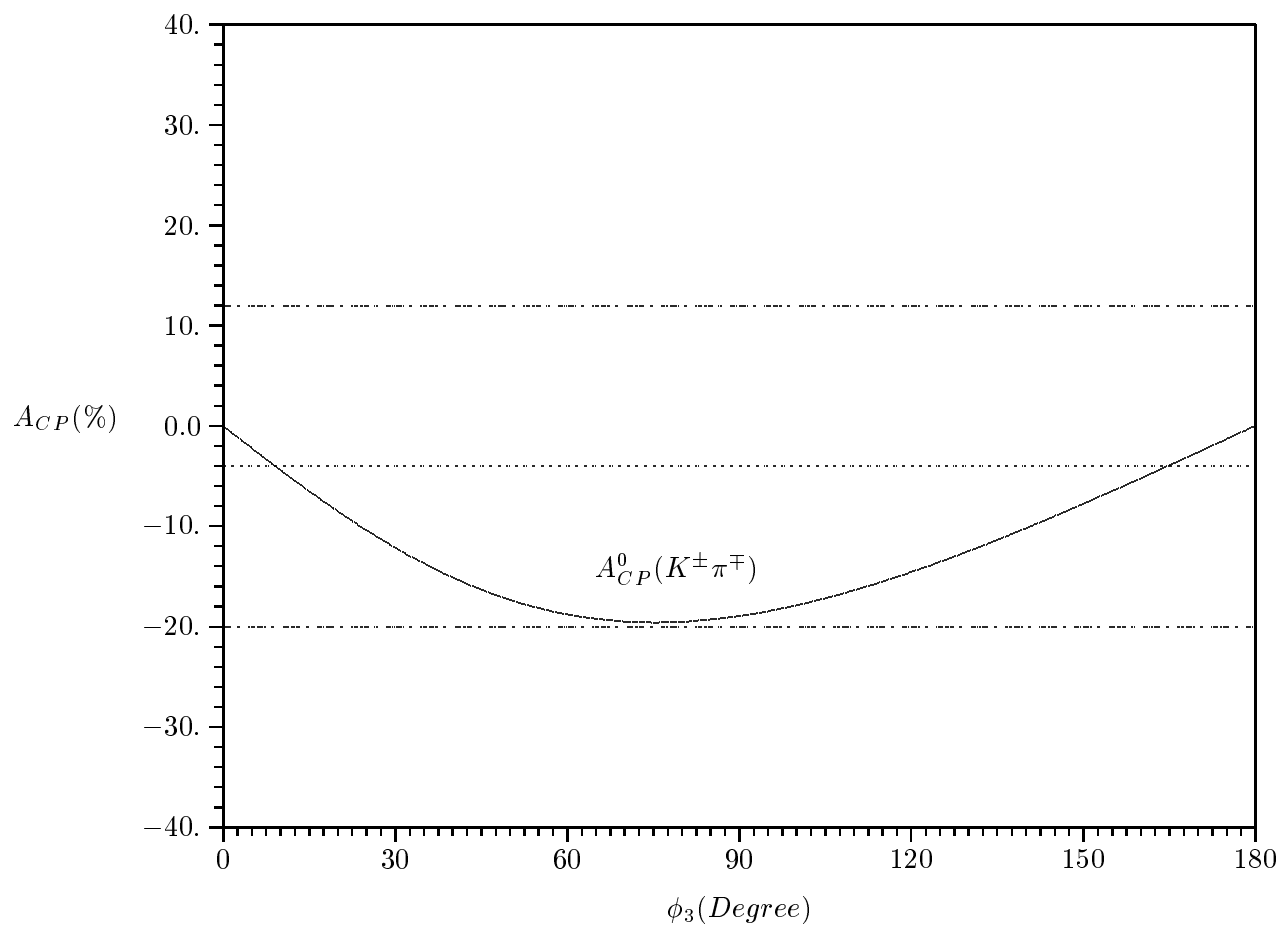


Figure 7(b)

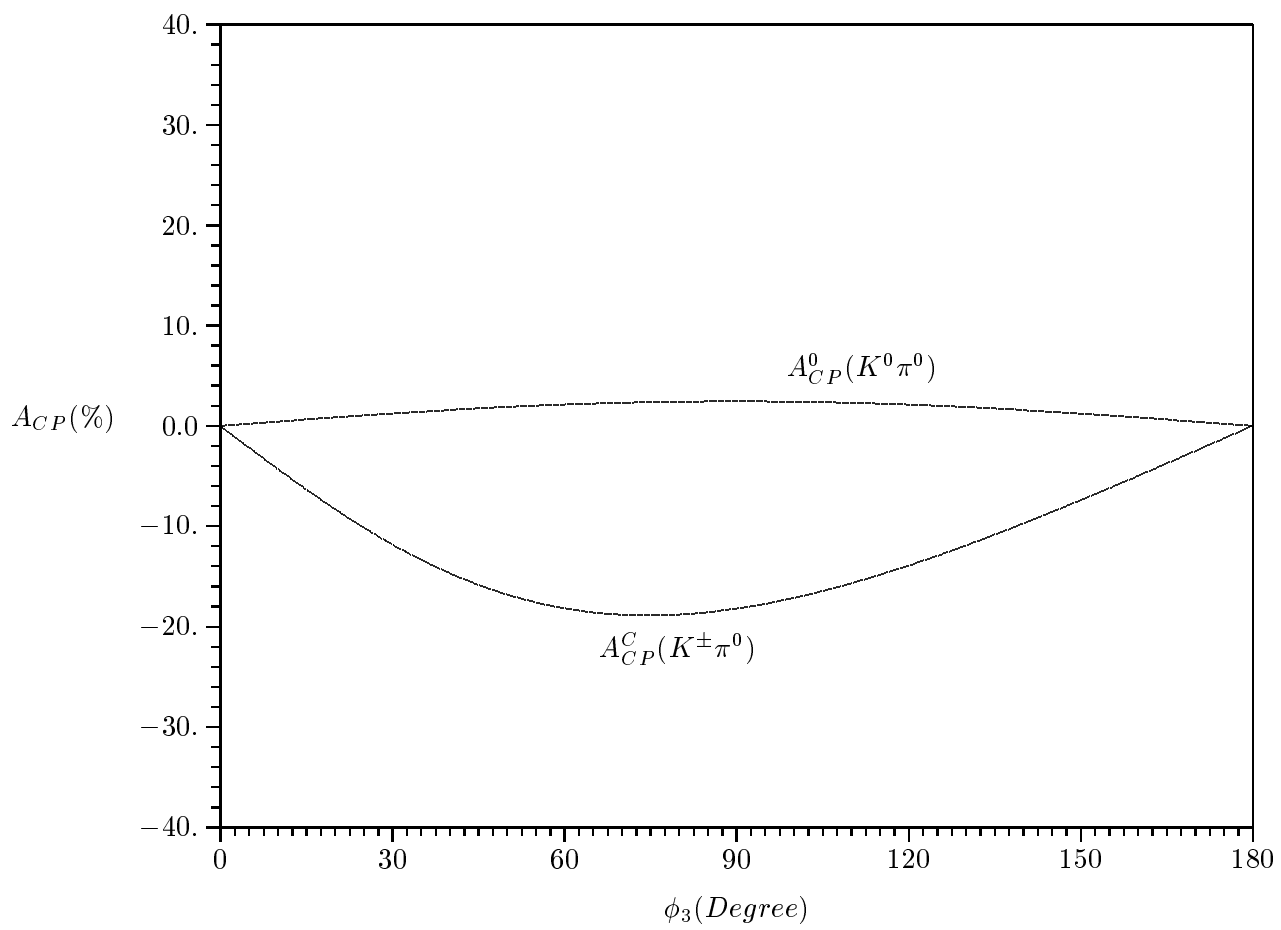


Figure 7(c)

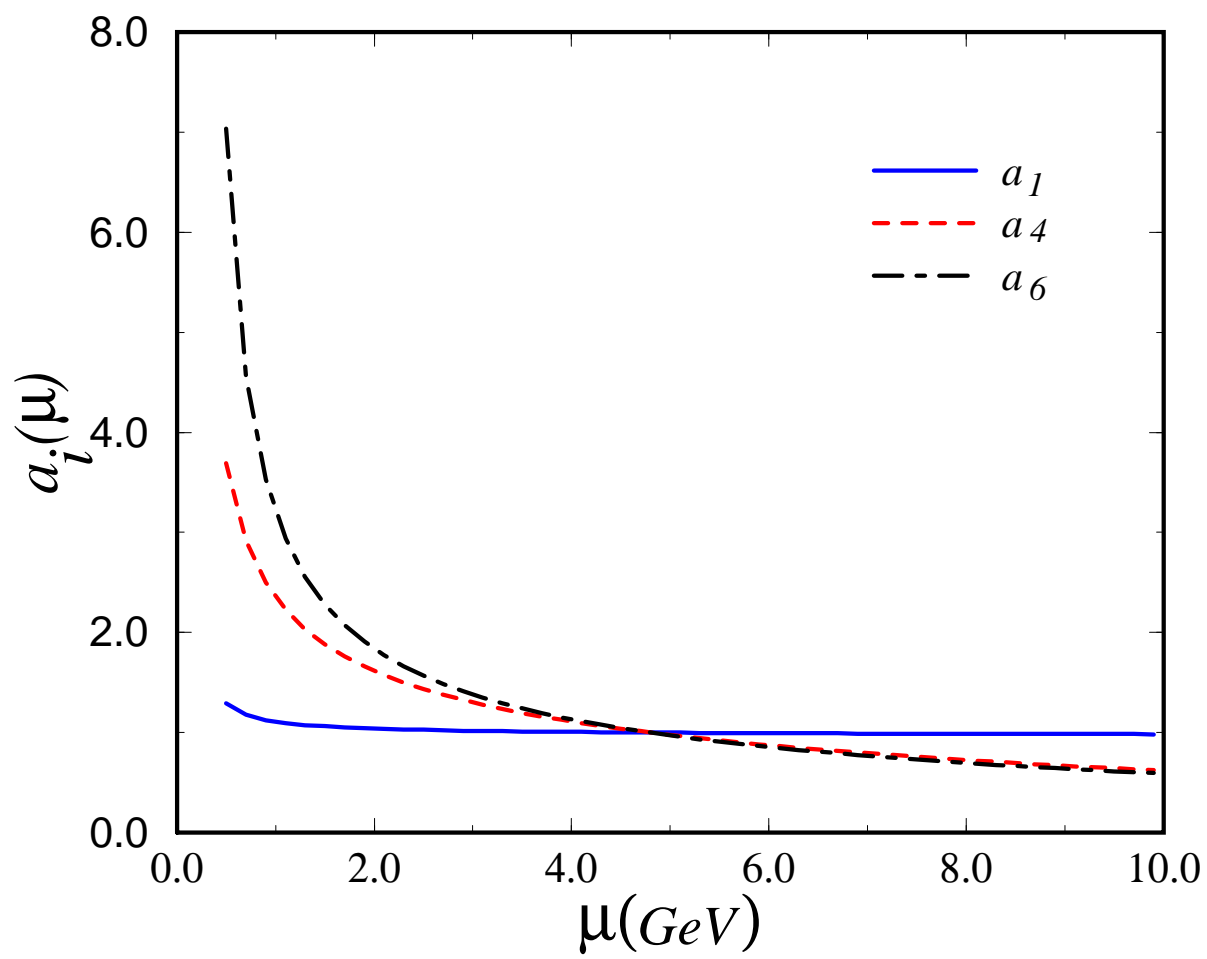


Figure 8

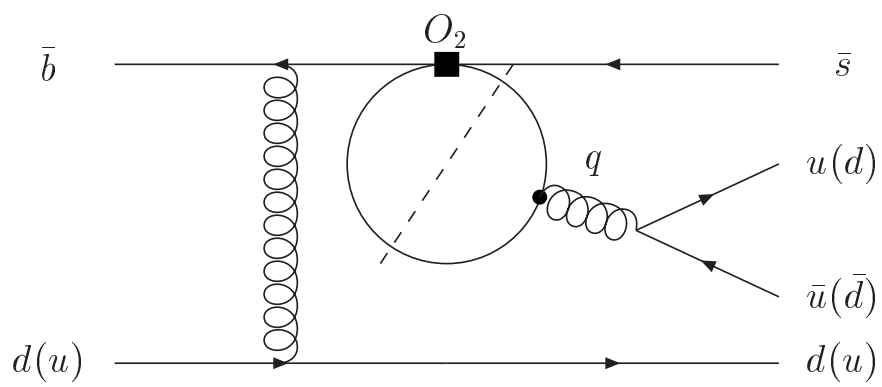


Figure 9:

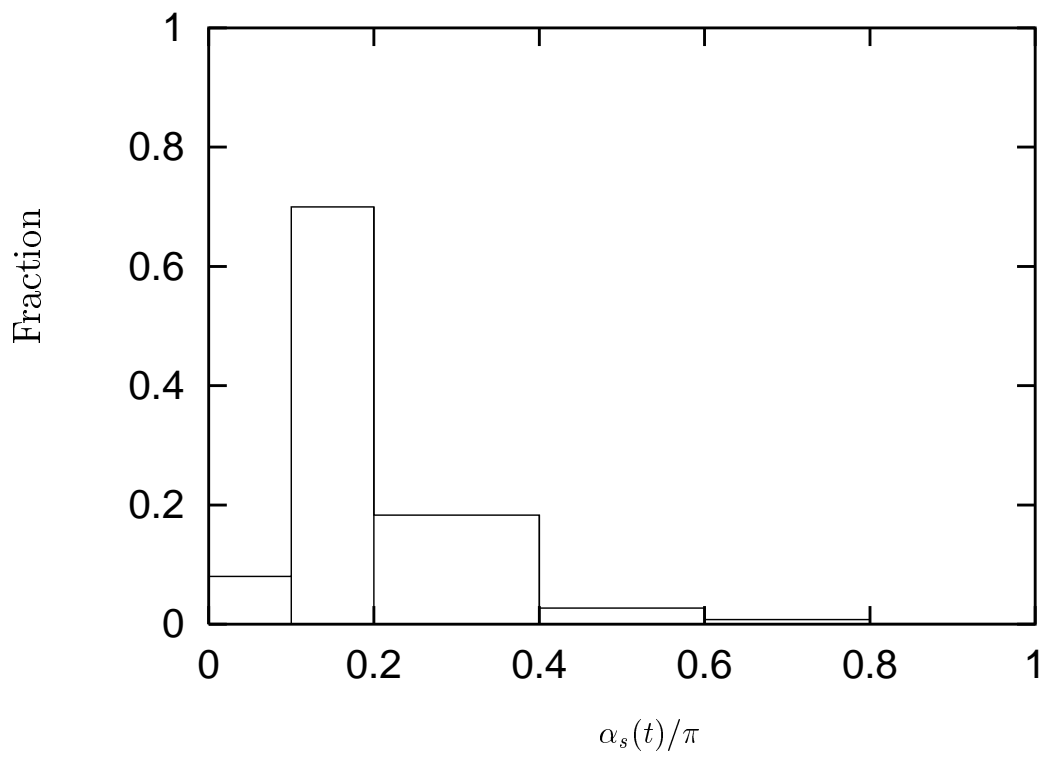


Figure 10: